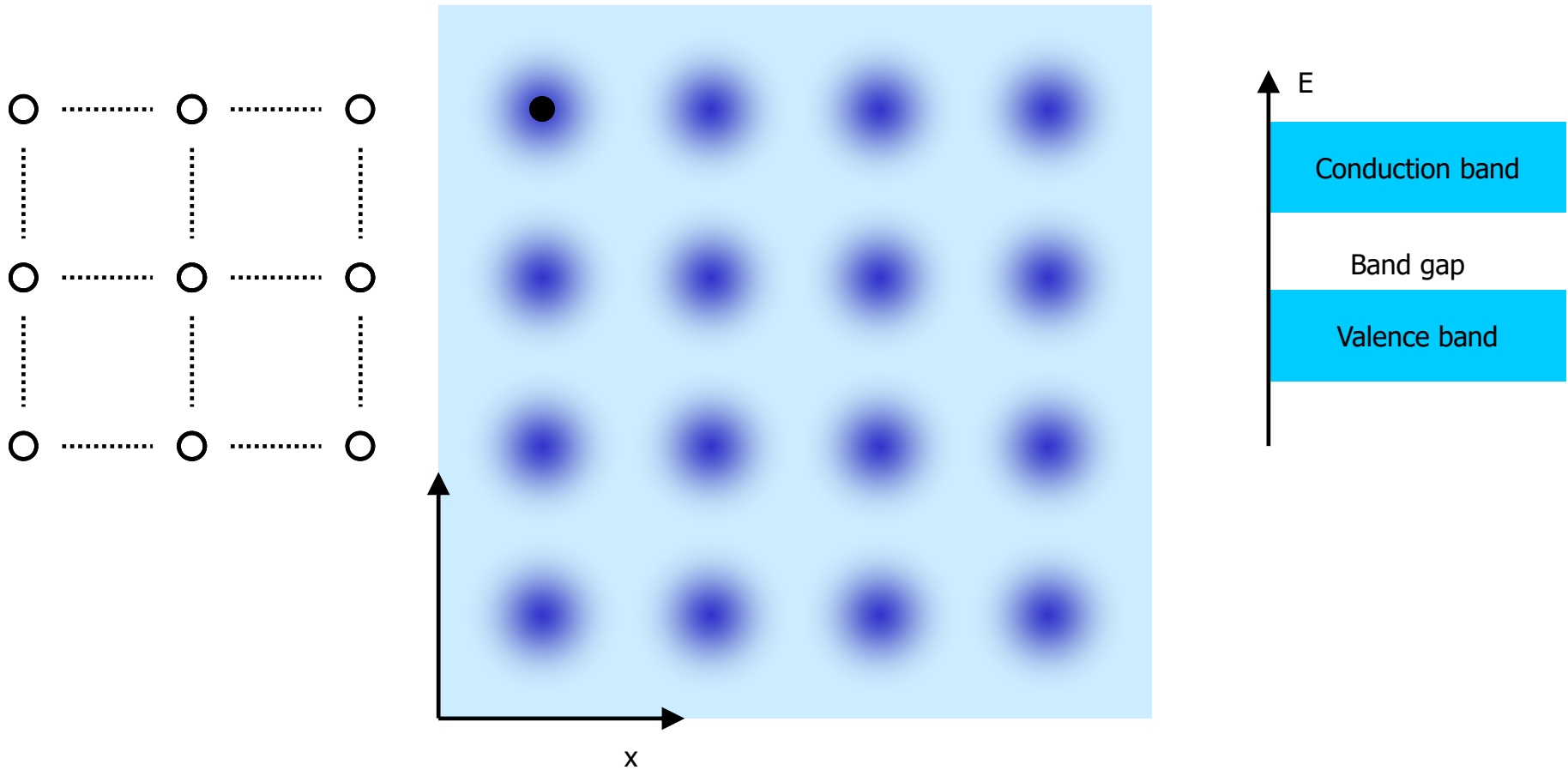
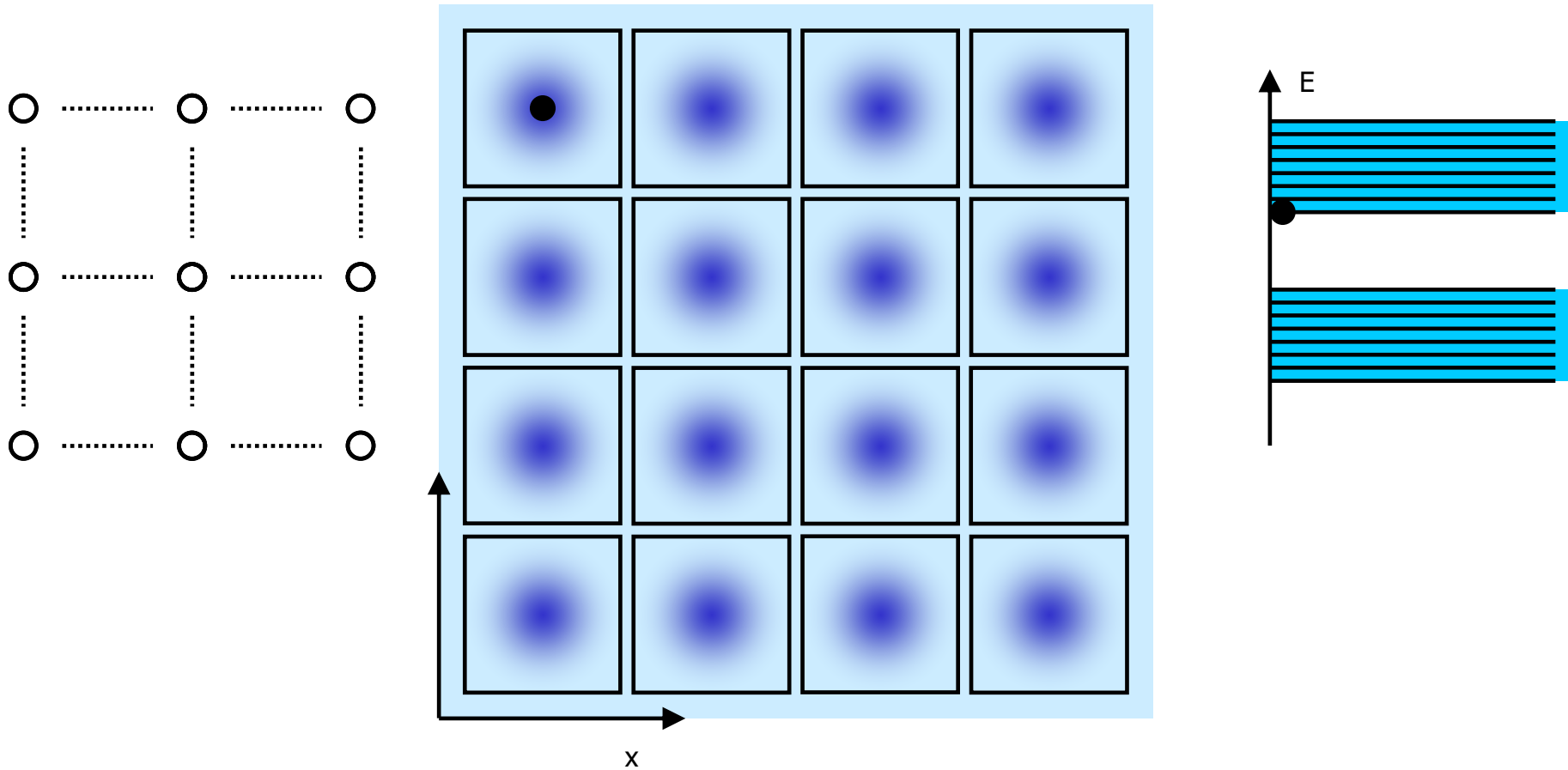

Advanced MOSFET Modelling

MOS Transistor

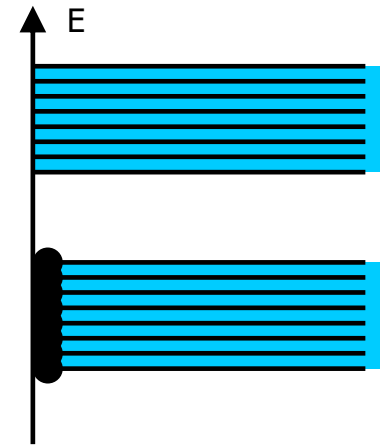
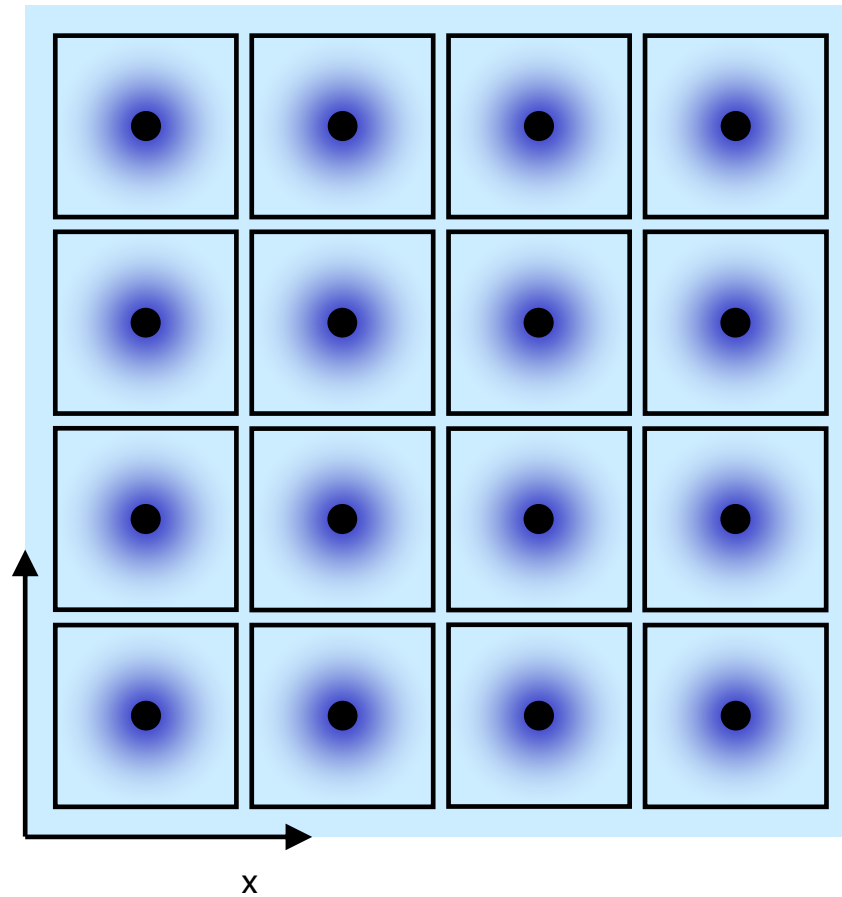
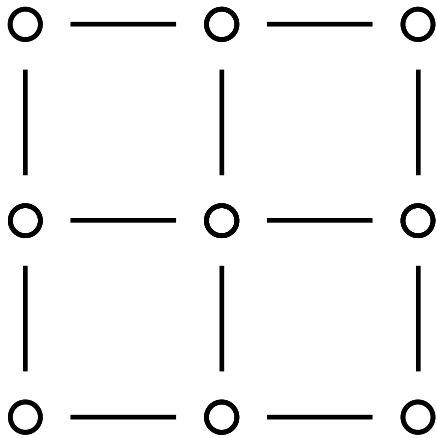
Text is in separated file!!!!



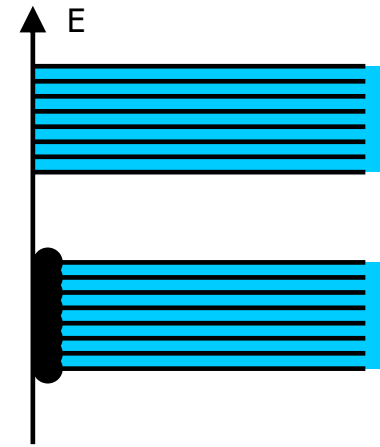
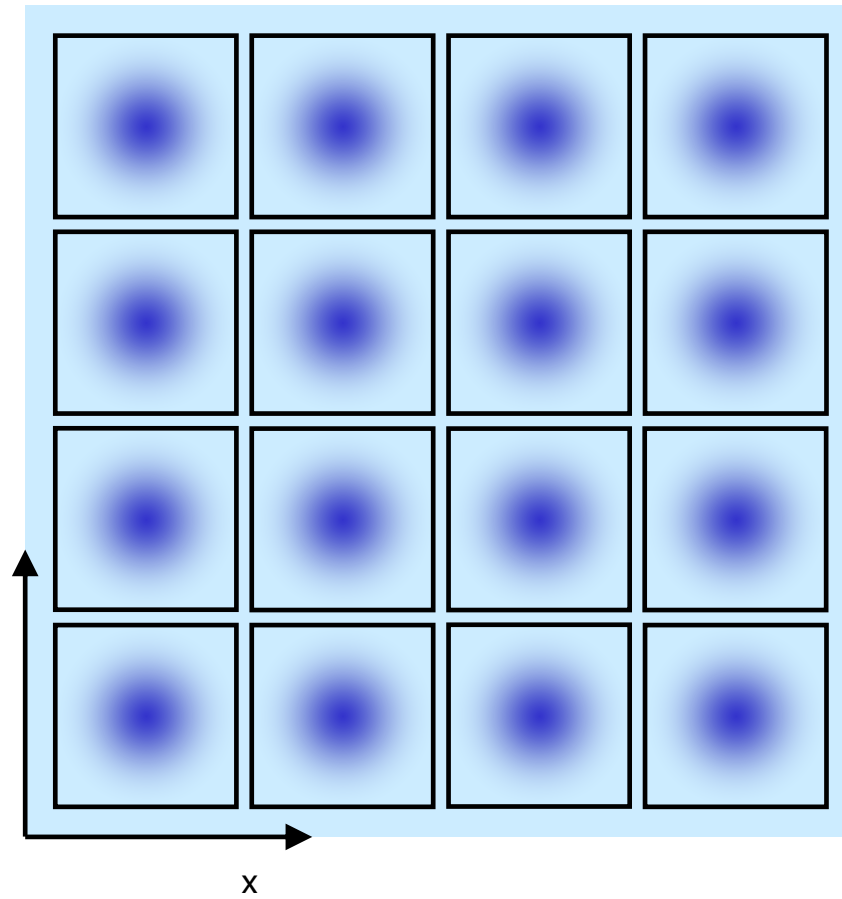
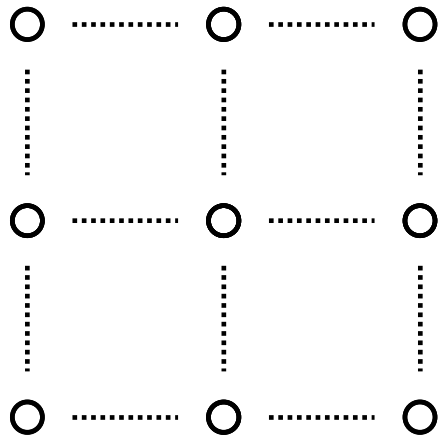
MOS Transistor



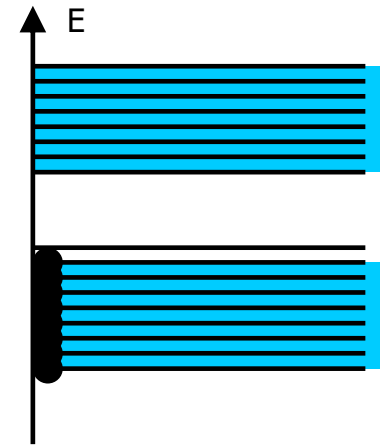
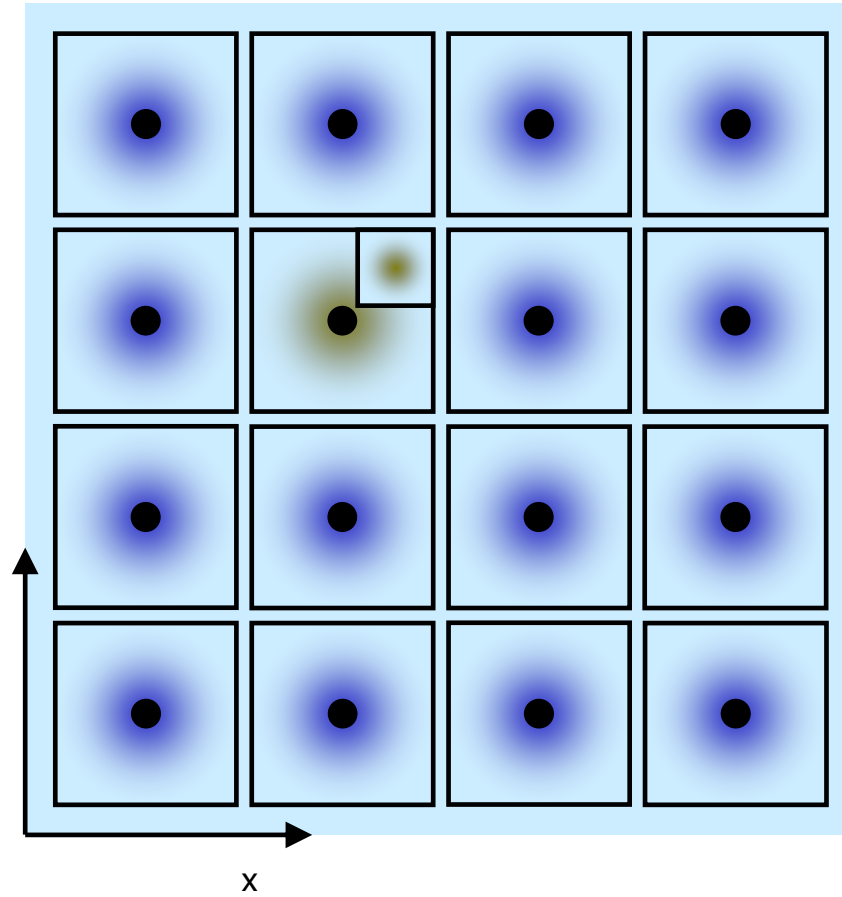
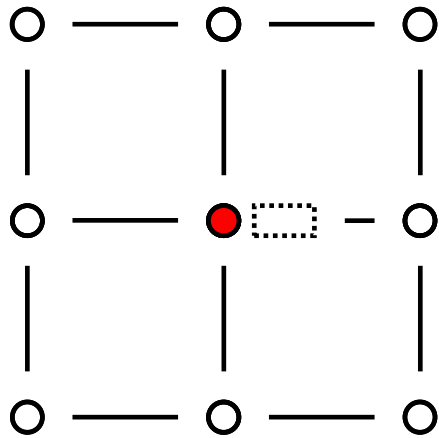
MOS Transistor



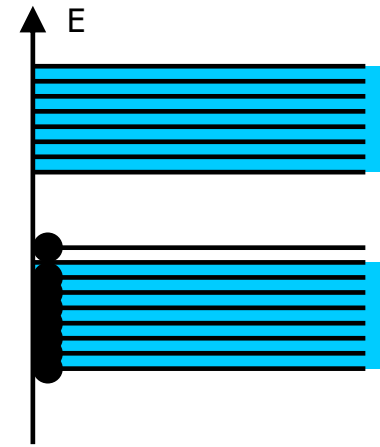
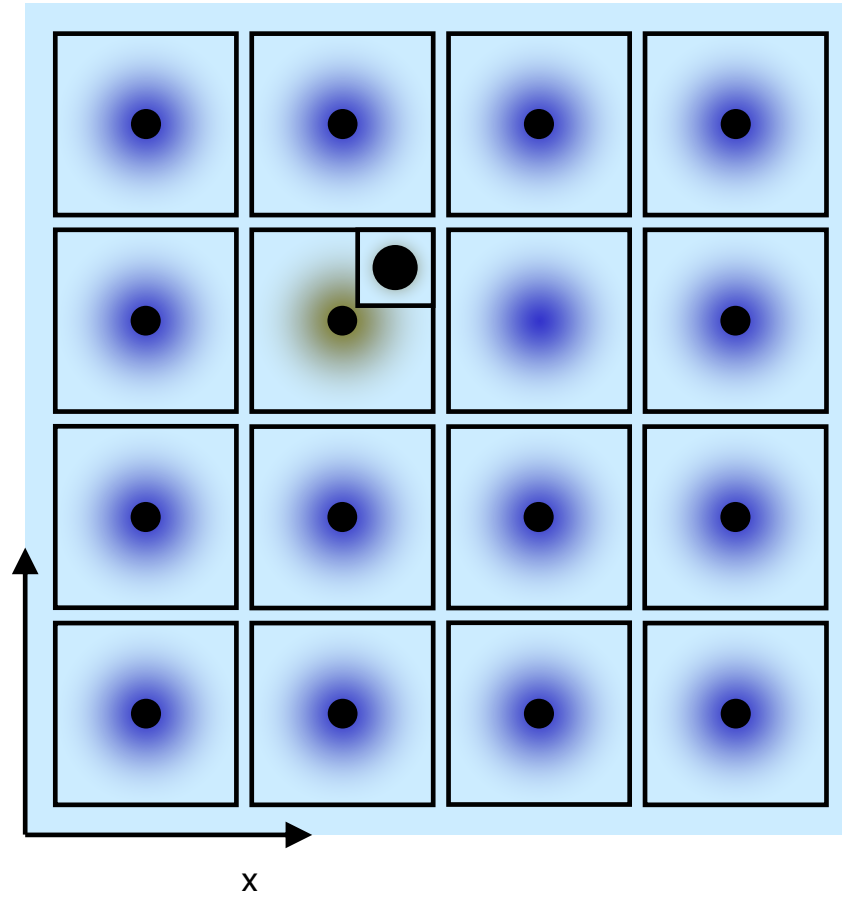
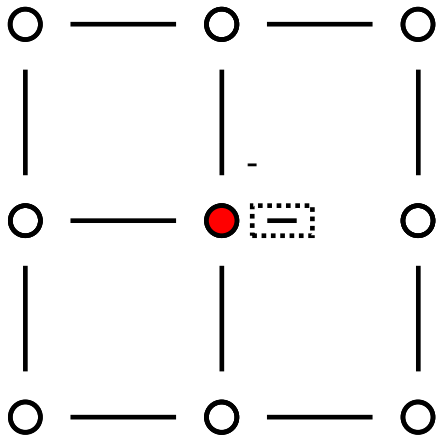
MOS Transistor



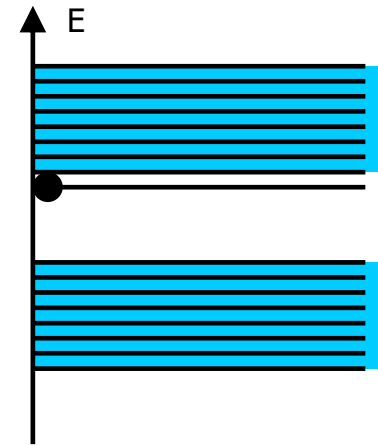
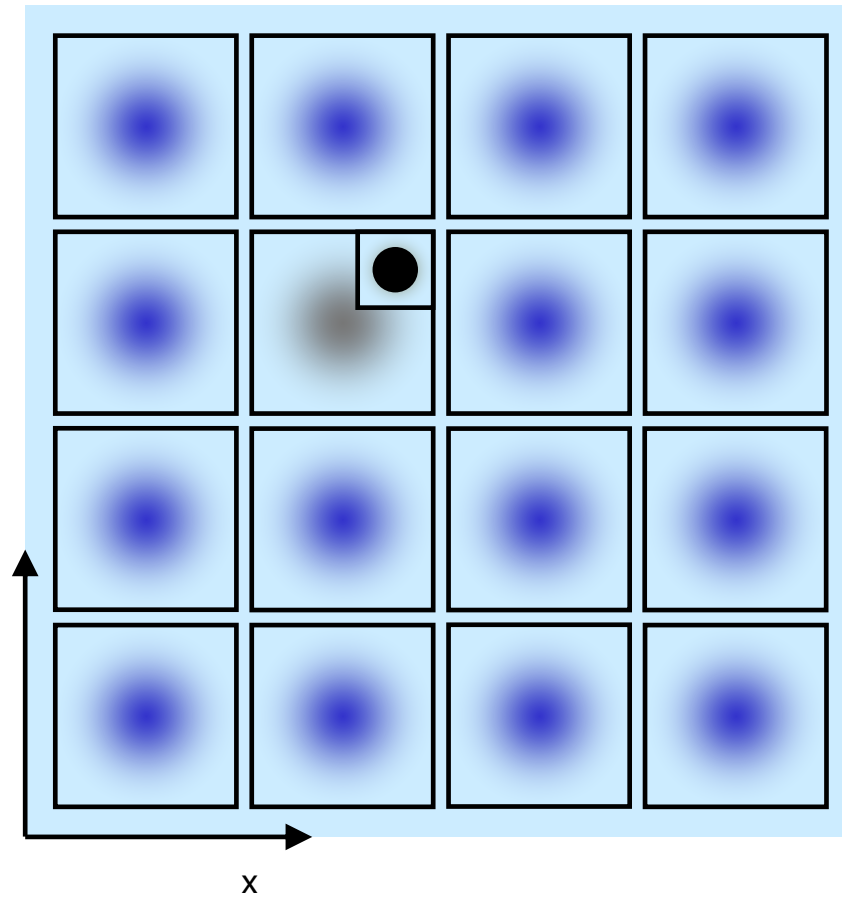
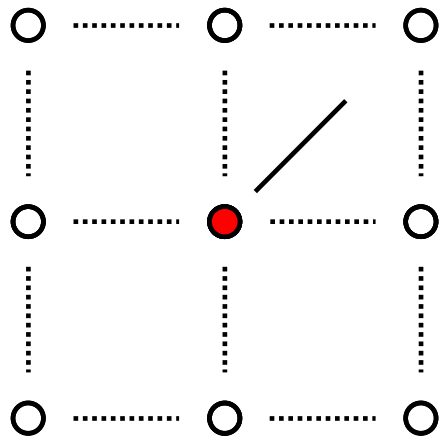
MOS Transistor



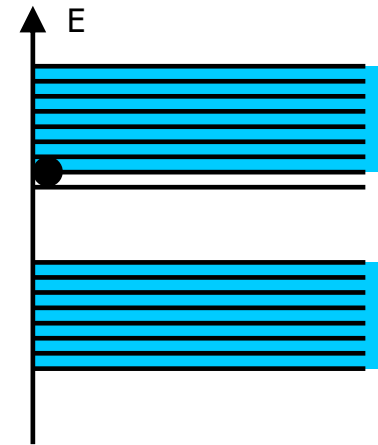
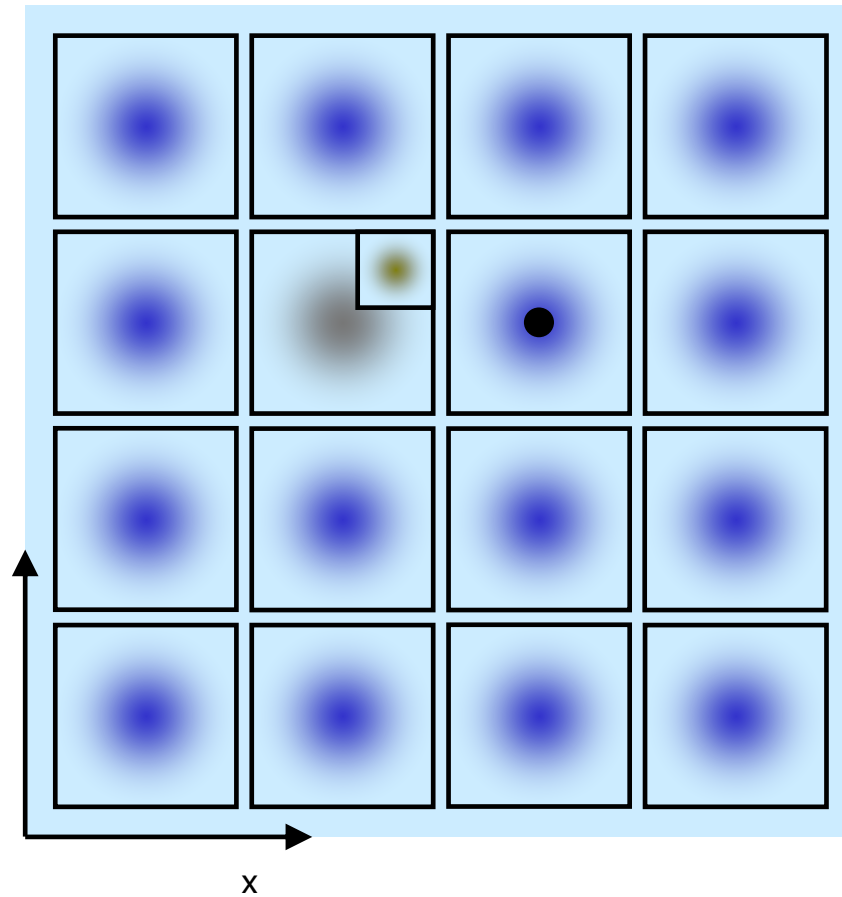
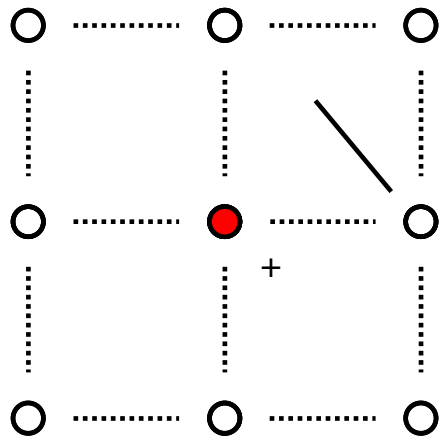
MOS Transistor



MOS Transistor



MOS Transistor

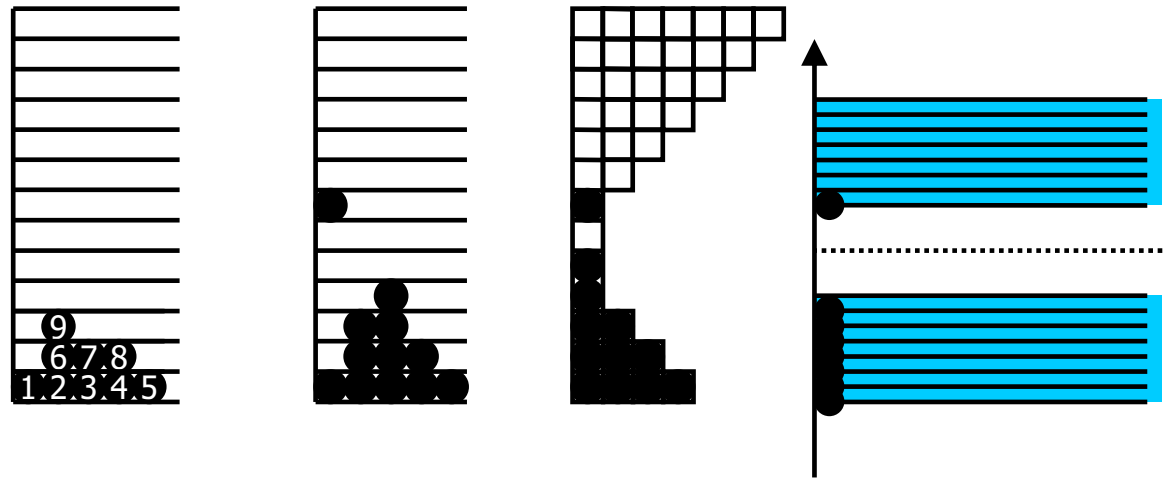


MOS Transistor

$$n = n_0 e^{-\frac{E}{kT}}$$

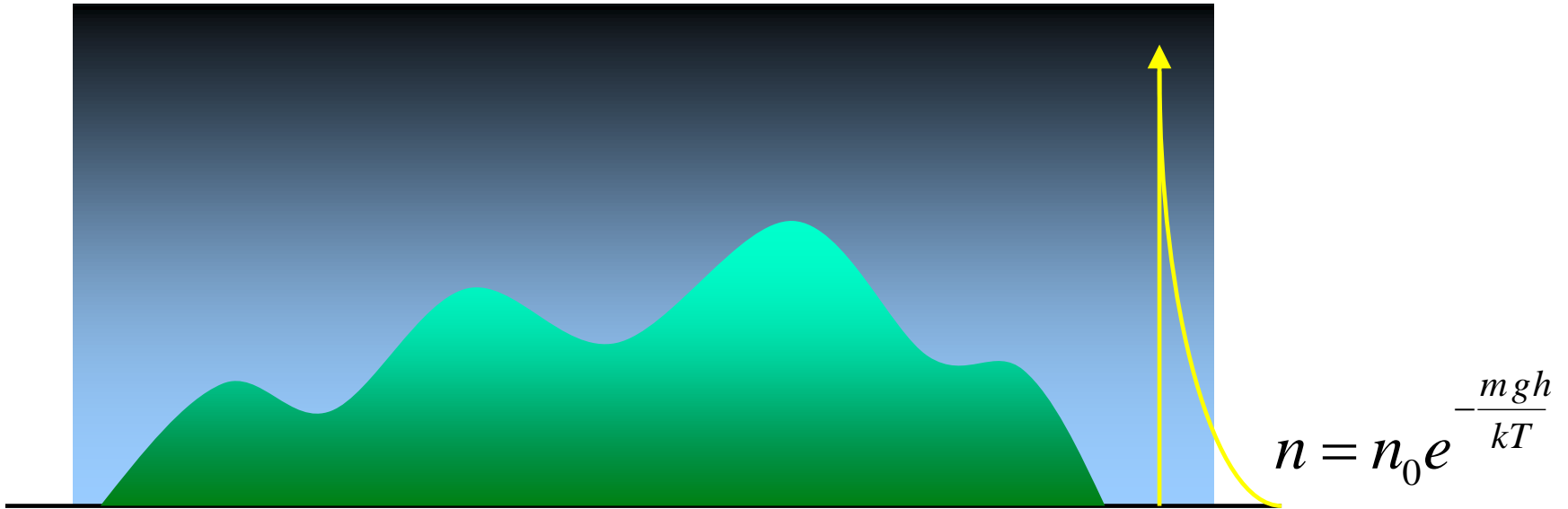
$$n = \frac{1}{e^{\frac{E-\mu}{kT}} - 1}$$

$$n = \frac{1}{e^{\frac{E-E_f}{kT}} + 1}$$

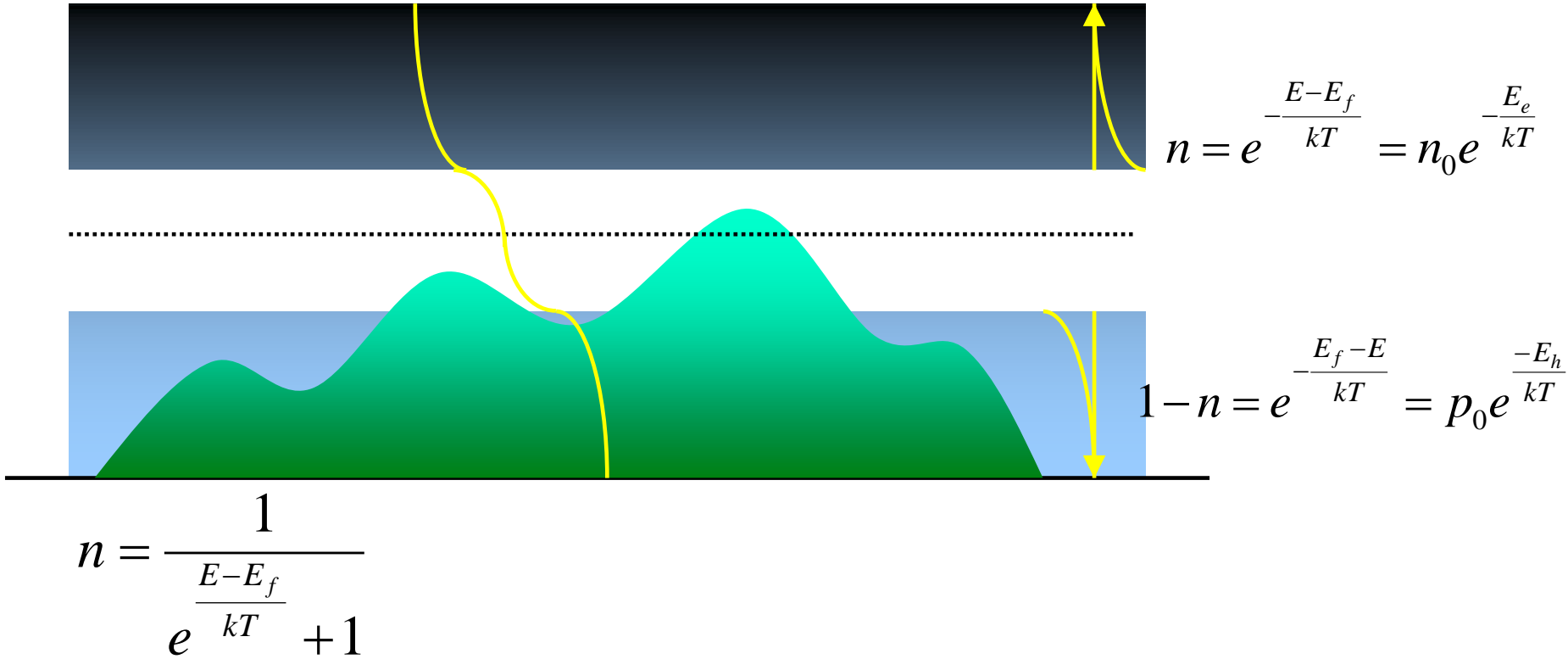


Maxwell-Boltzmann Distribution

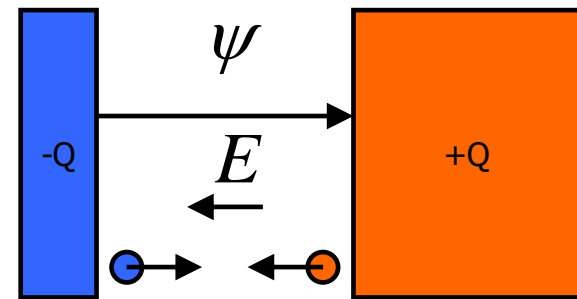
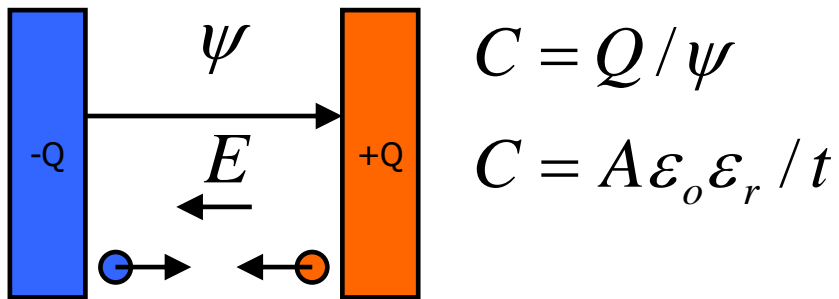
$$n = n_0 e^{-\frac{E}{kT}}$$



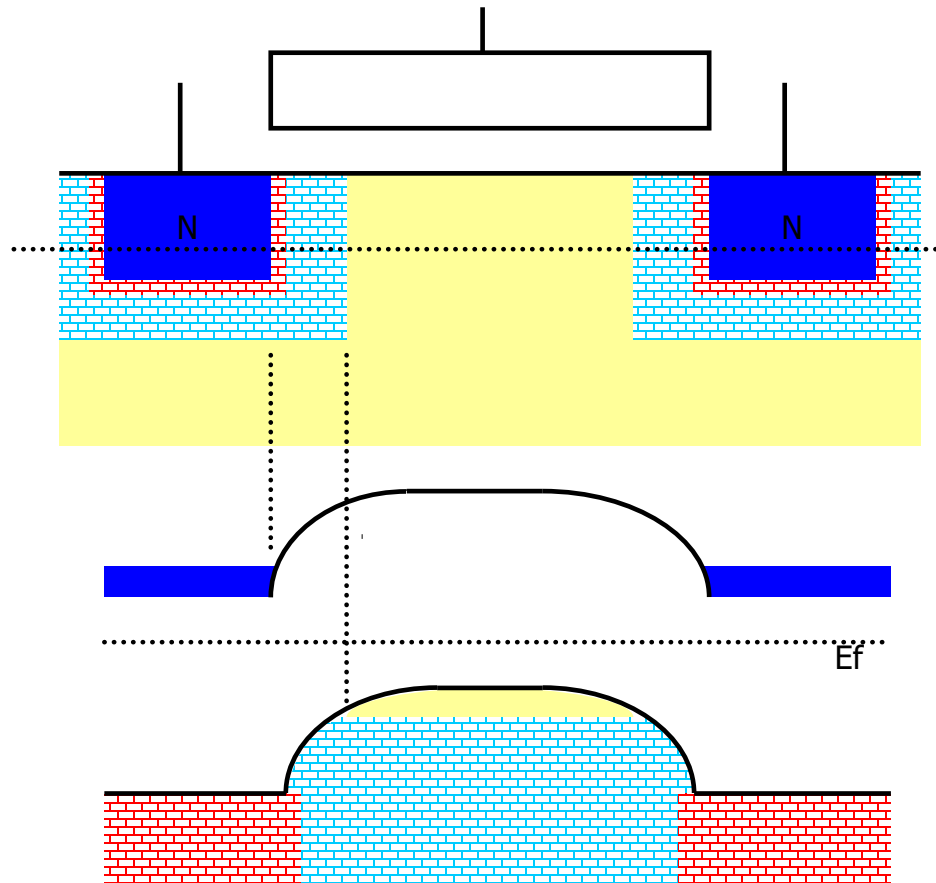
Maxwell-Boltzmann Distribution



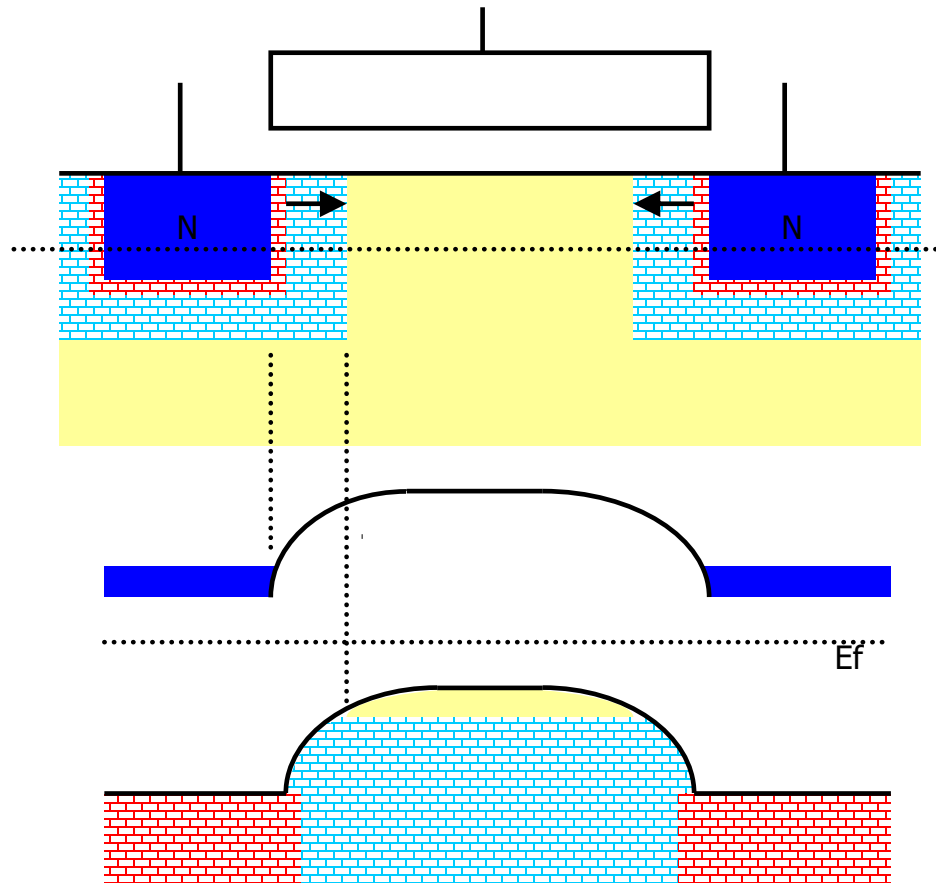
Maxwell-Boltzmann Distribution



MOS Transistor

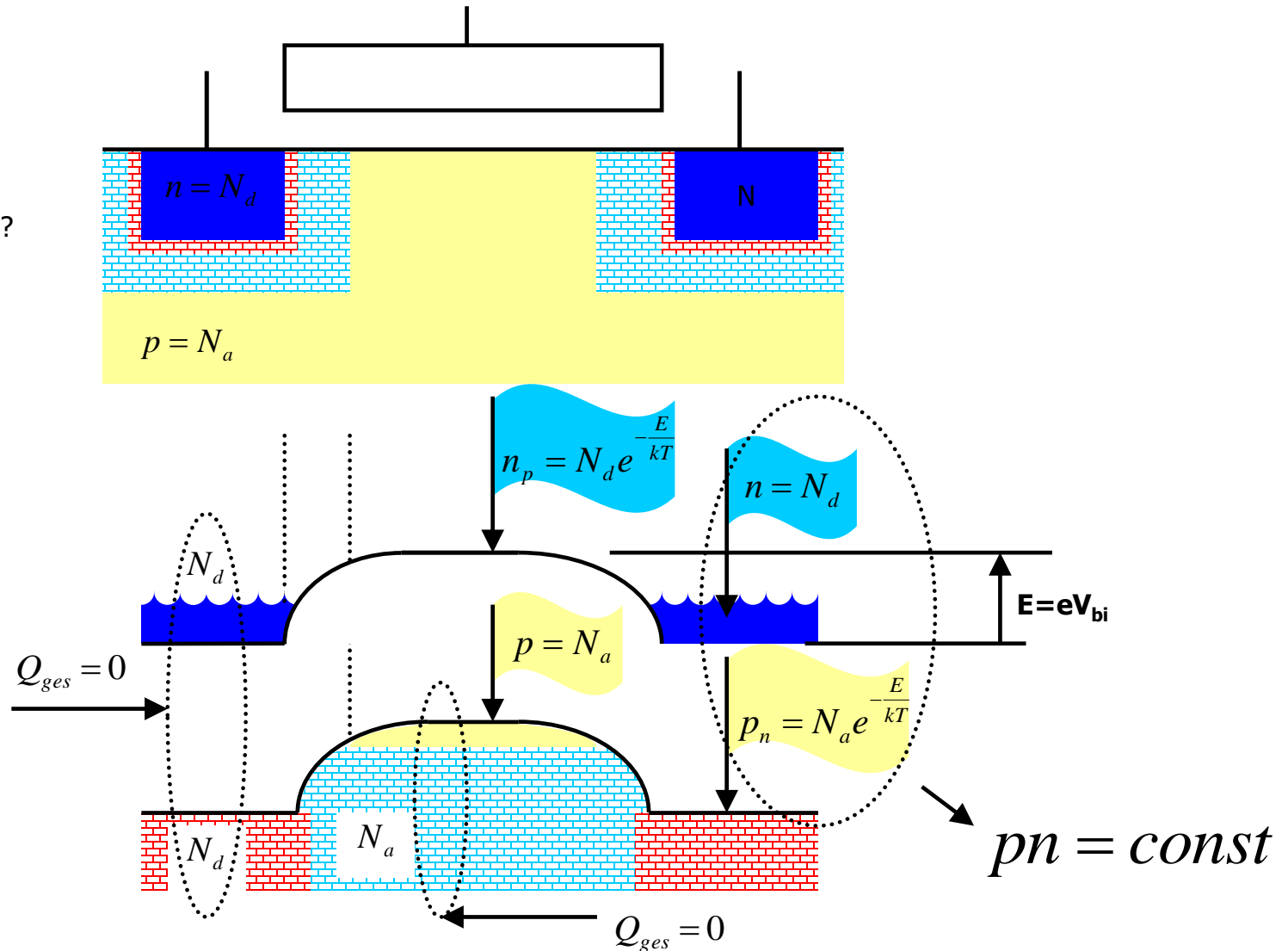


MOS Transistor



MOS Transistor – Carrier Density

Warum Sperrzone?



Intrinsic Semiconductor

TDG

$$pn = \text{const}$$

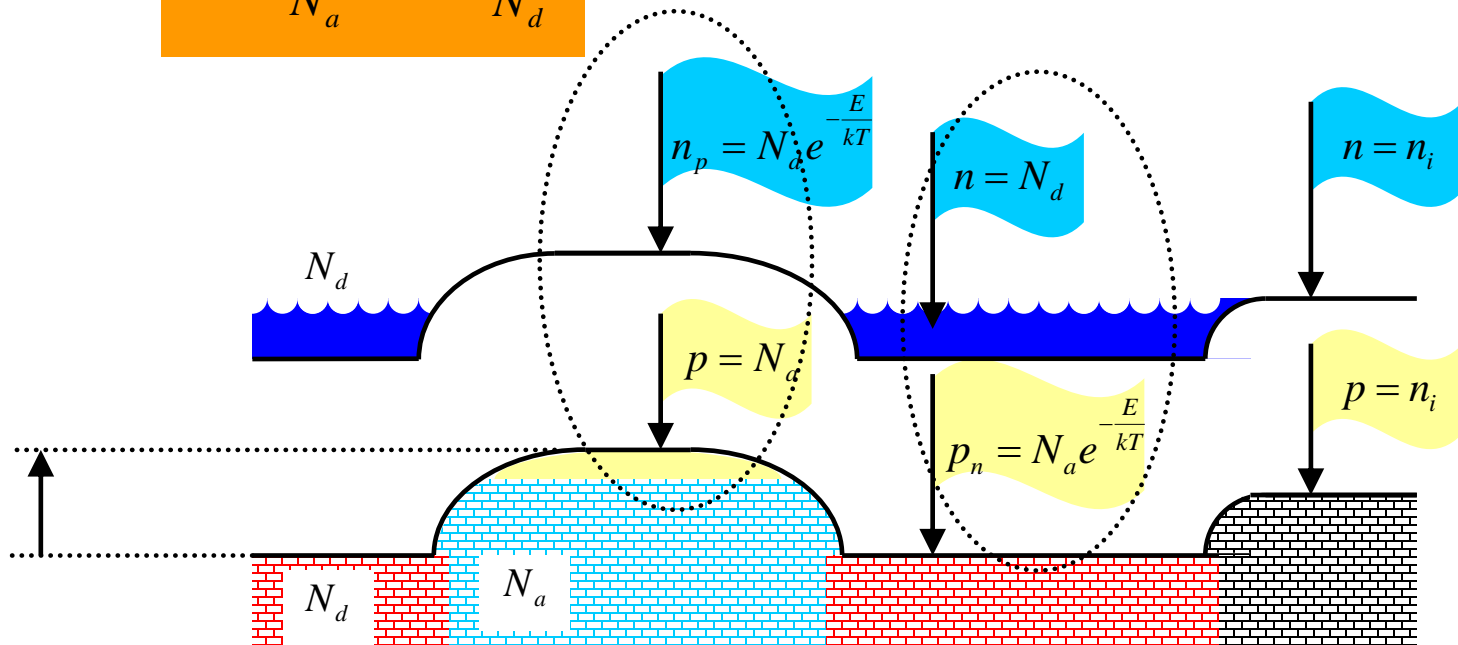
$$pn = n_i^2$$

$$n_i = 1.45 \times 10^{10} \text{ cm}^{-3}$$

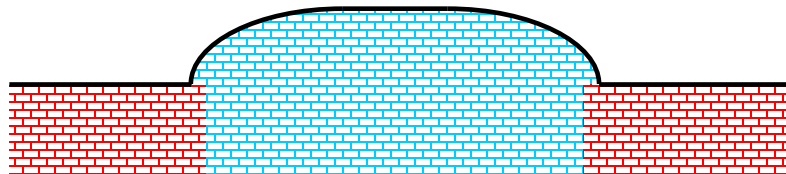
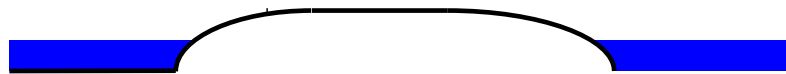
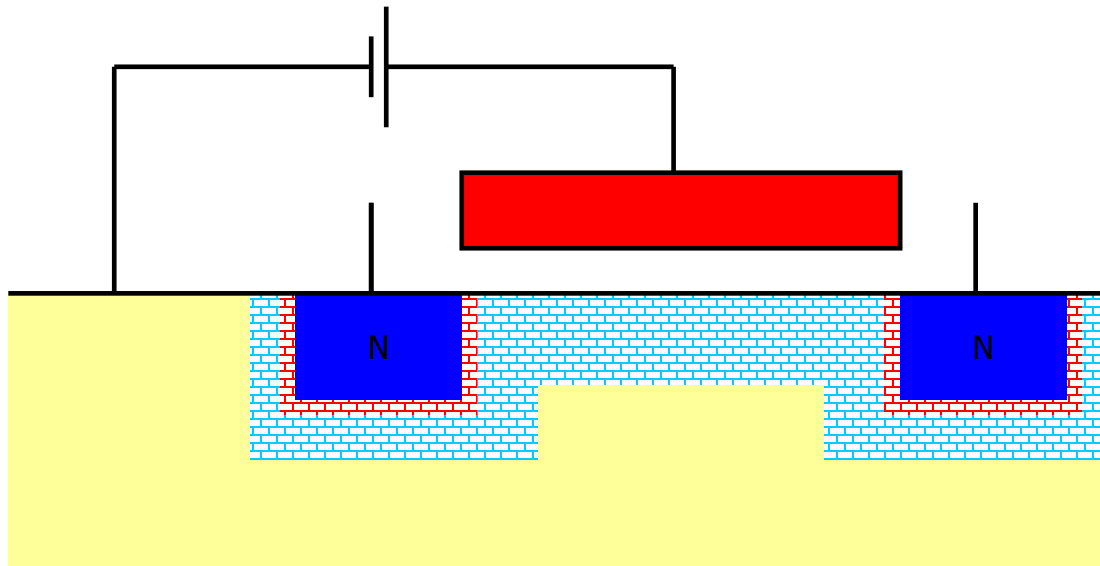
$$n_{\text{atom}\xi} \approx 10^{22} \text{ cm}^{-3}$$

$$N_a, N_d \approx 10^{16} \text{ cm}^{-3}$$

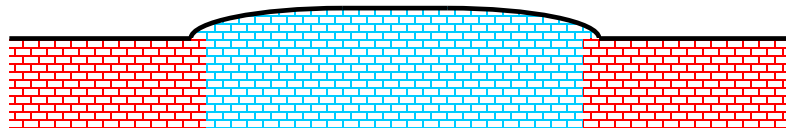
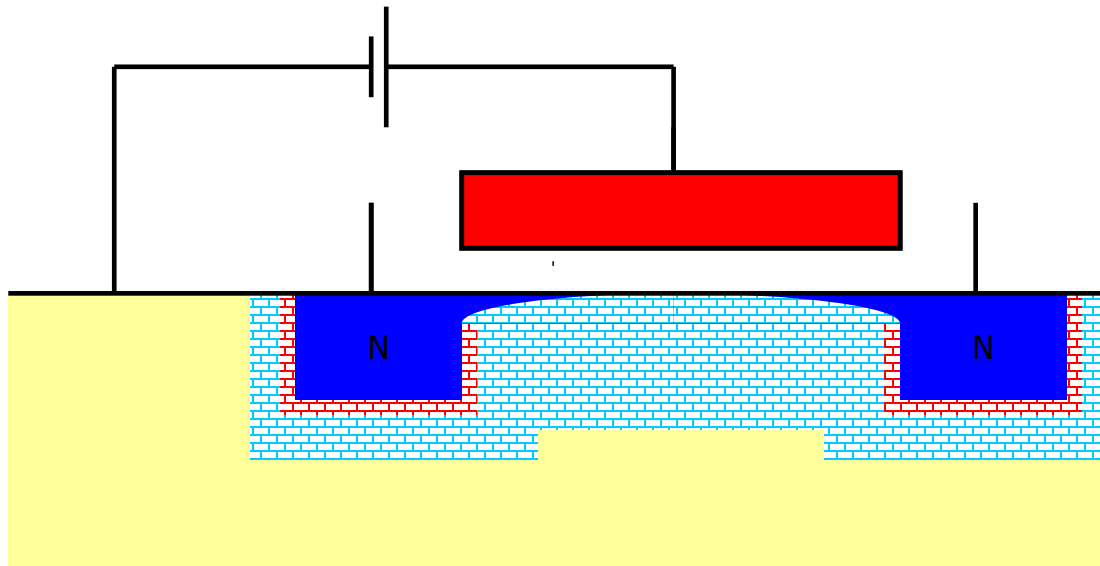
$$n_{p0} = \frac{n_i^2}{N_a} \quad p_{n0} = \frac{n_i^2}{N_d}$$



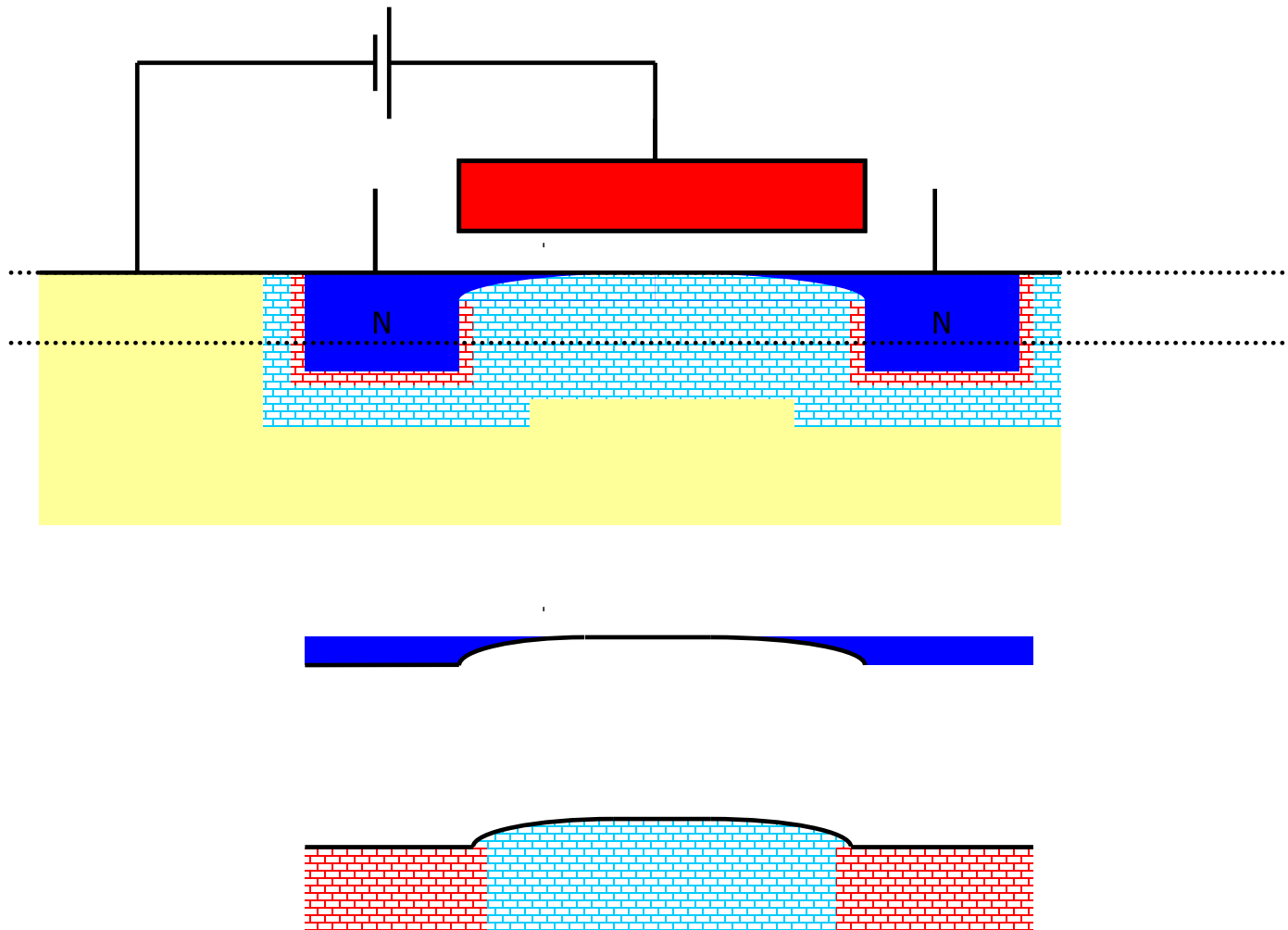
Gate Voltage



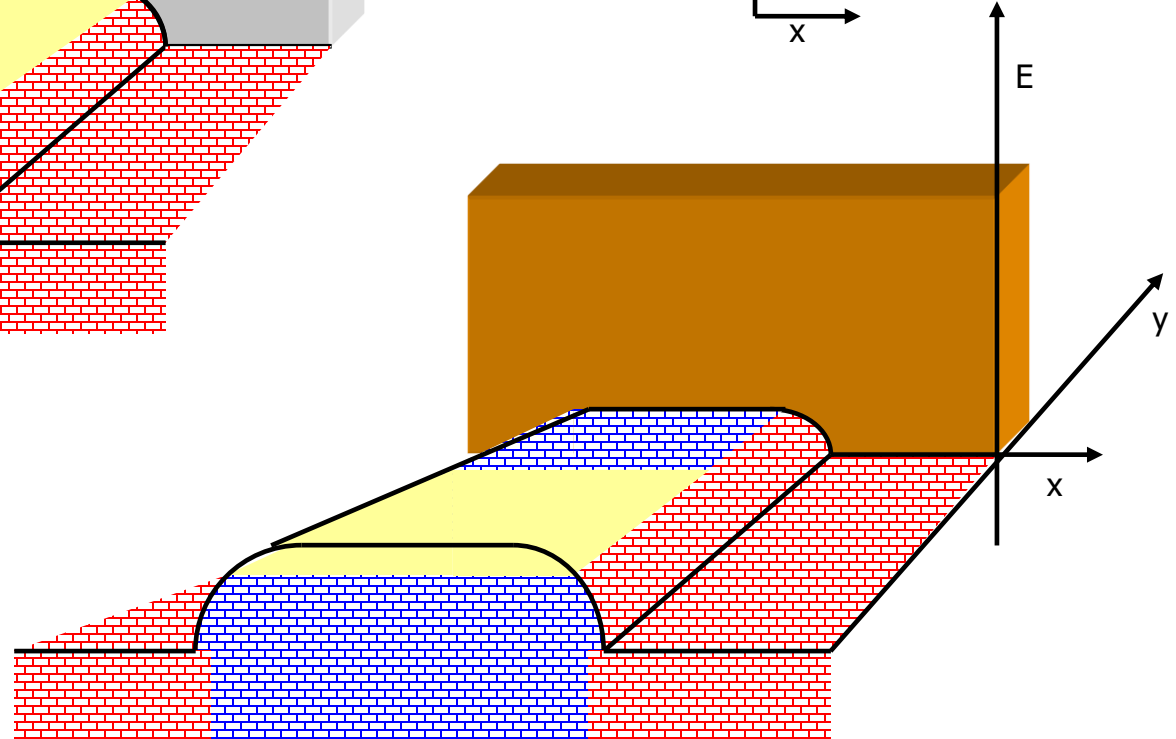
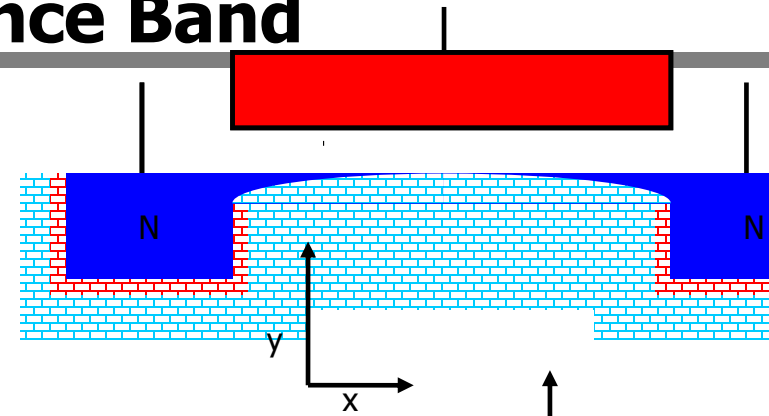
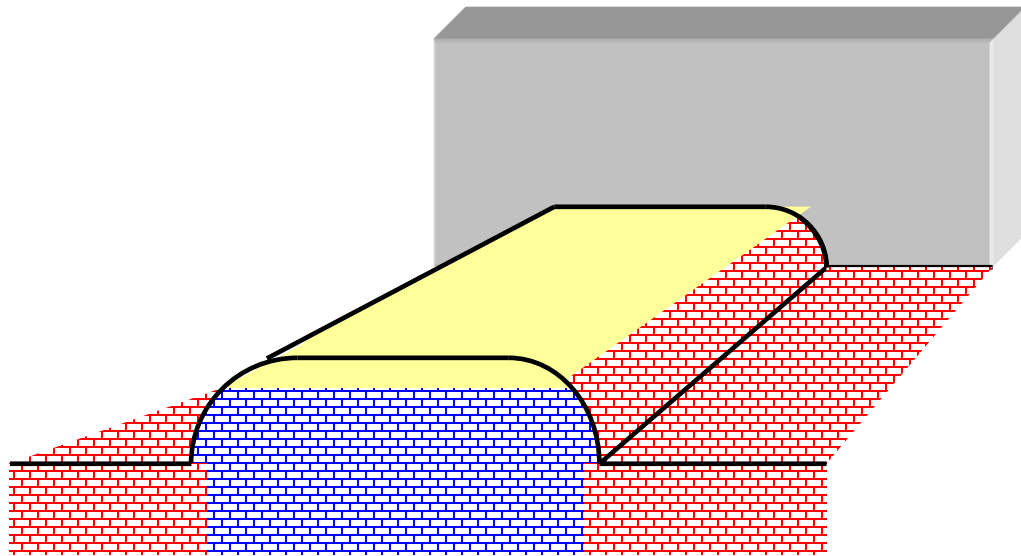
Gate Voltage - Channel



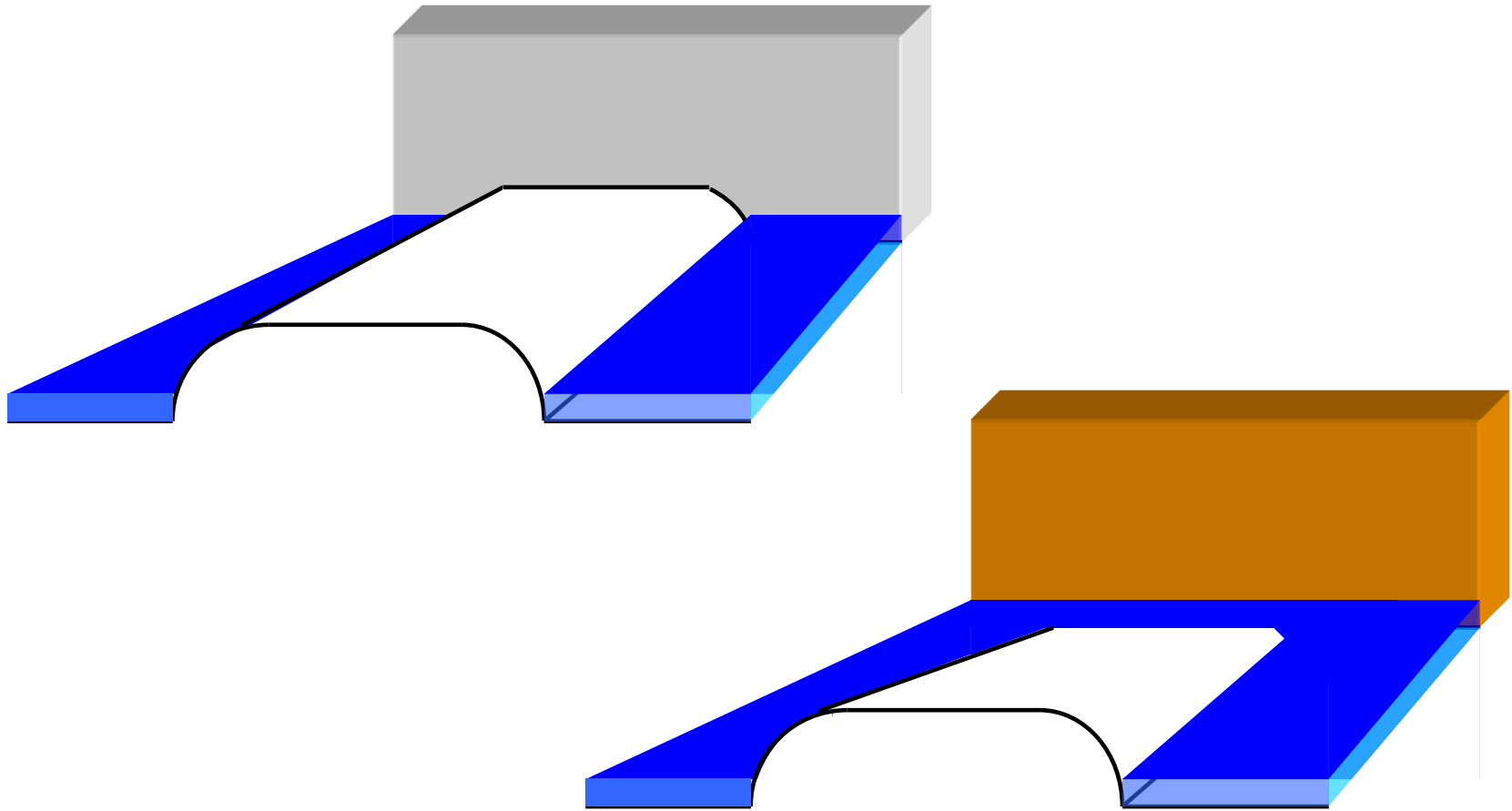
Gate Voltage



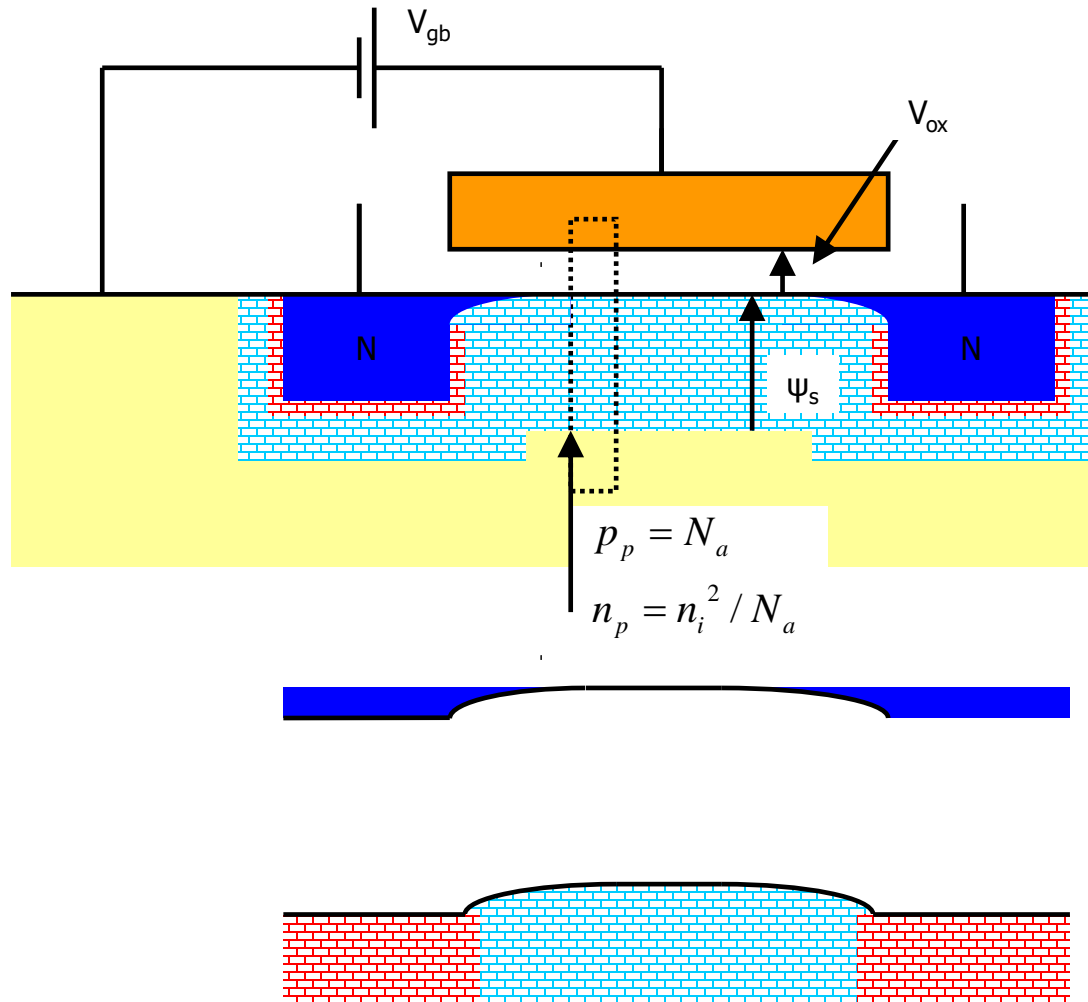
Gate Voltage – Valence Band



Gate Voltage – Conduction Band

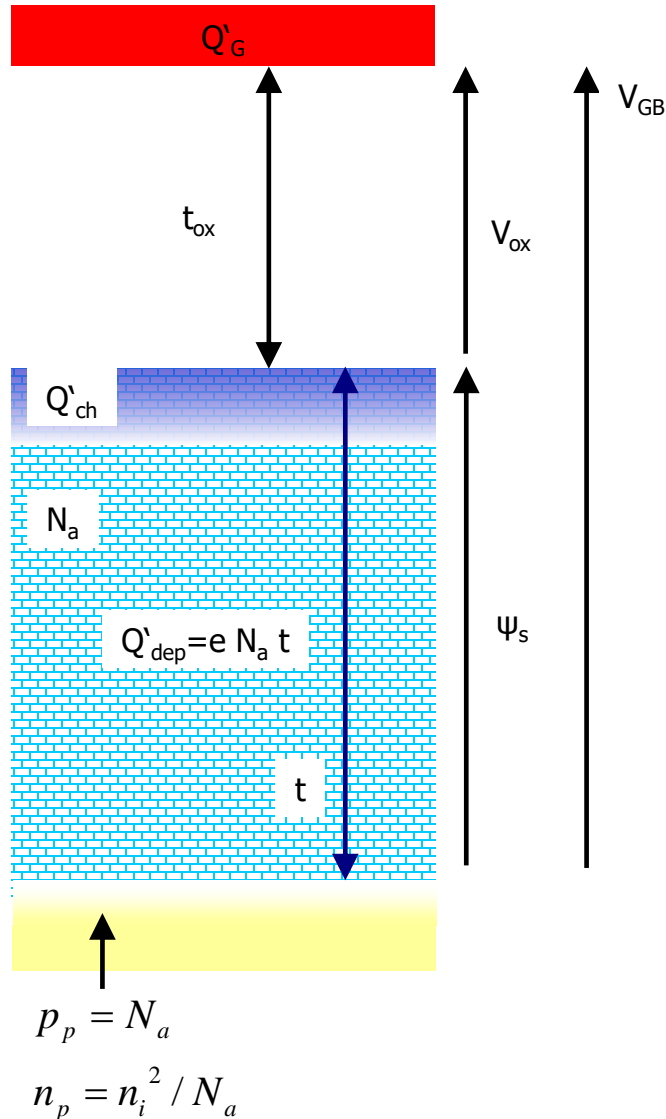


Gate Voltage – Electron Density in Channel



Electron Density in Channel

Warum so steil?



$$Q'_{ch}(V_{GB}) = ?$$

$$V_{GB} = \psi_s + V_{ox}$$

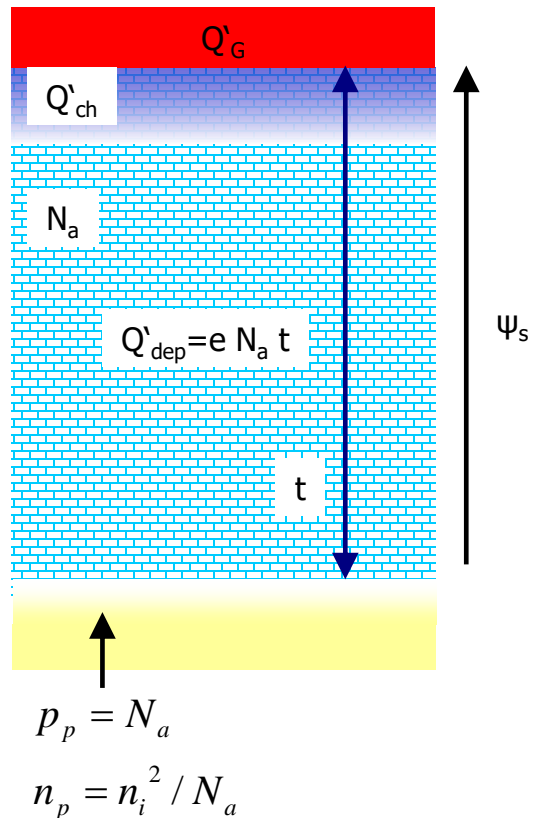
$$Q'_G = Q'_{ch} + Q'_{dep}$$

$$V_{ox} = \frac{Q'_G}{C'_{ox}} = \frac{Q'_{ch} + Q'_{dep}}{C'_{ox}} \quad C'_{ox} = \frac{\epsilon_{SiO_2} \epsilon_0}{t_{ox}}$$

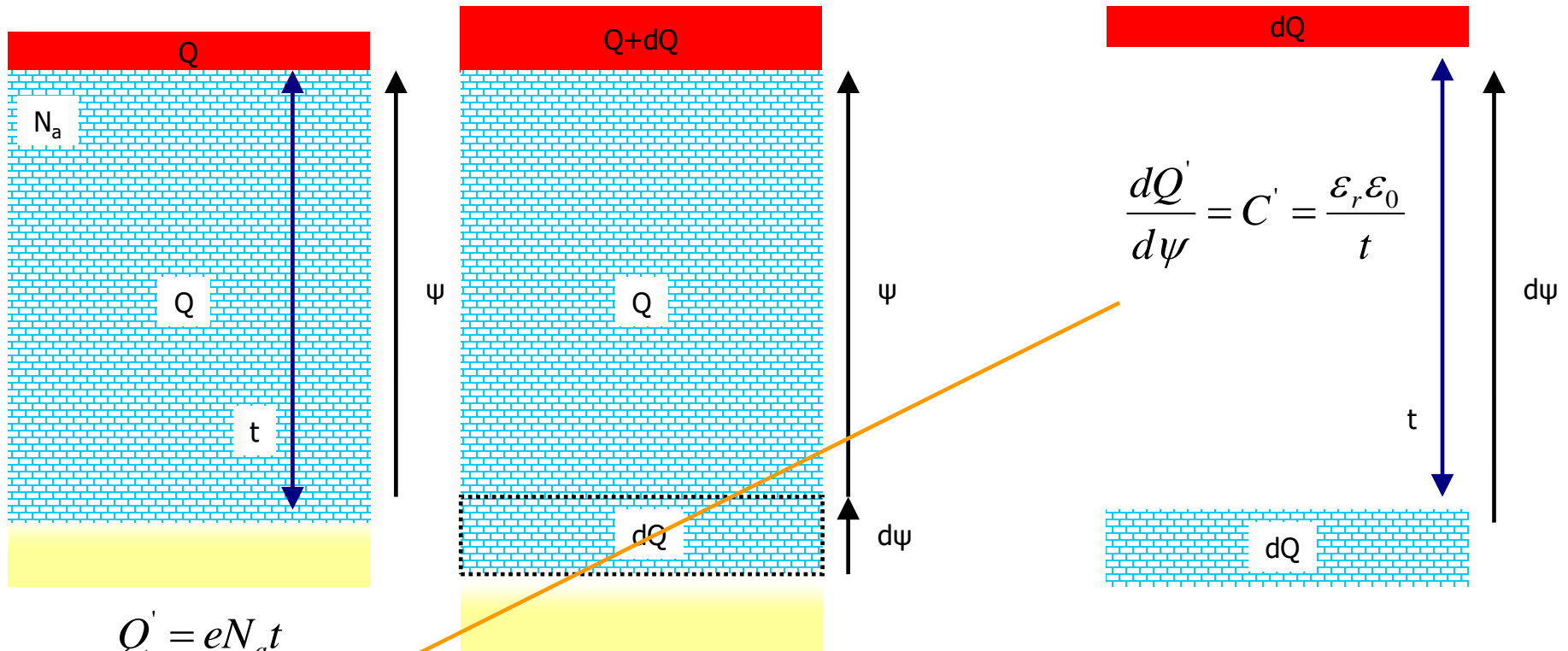
$$Q'_{ch}(\psi_s) = ?$$

$$Q'_{dep}(\psi_s) = ?$$

Gate Voltage – Electron Density in Channel



Charge in depleted Region



$$Q' = eN_a t$$

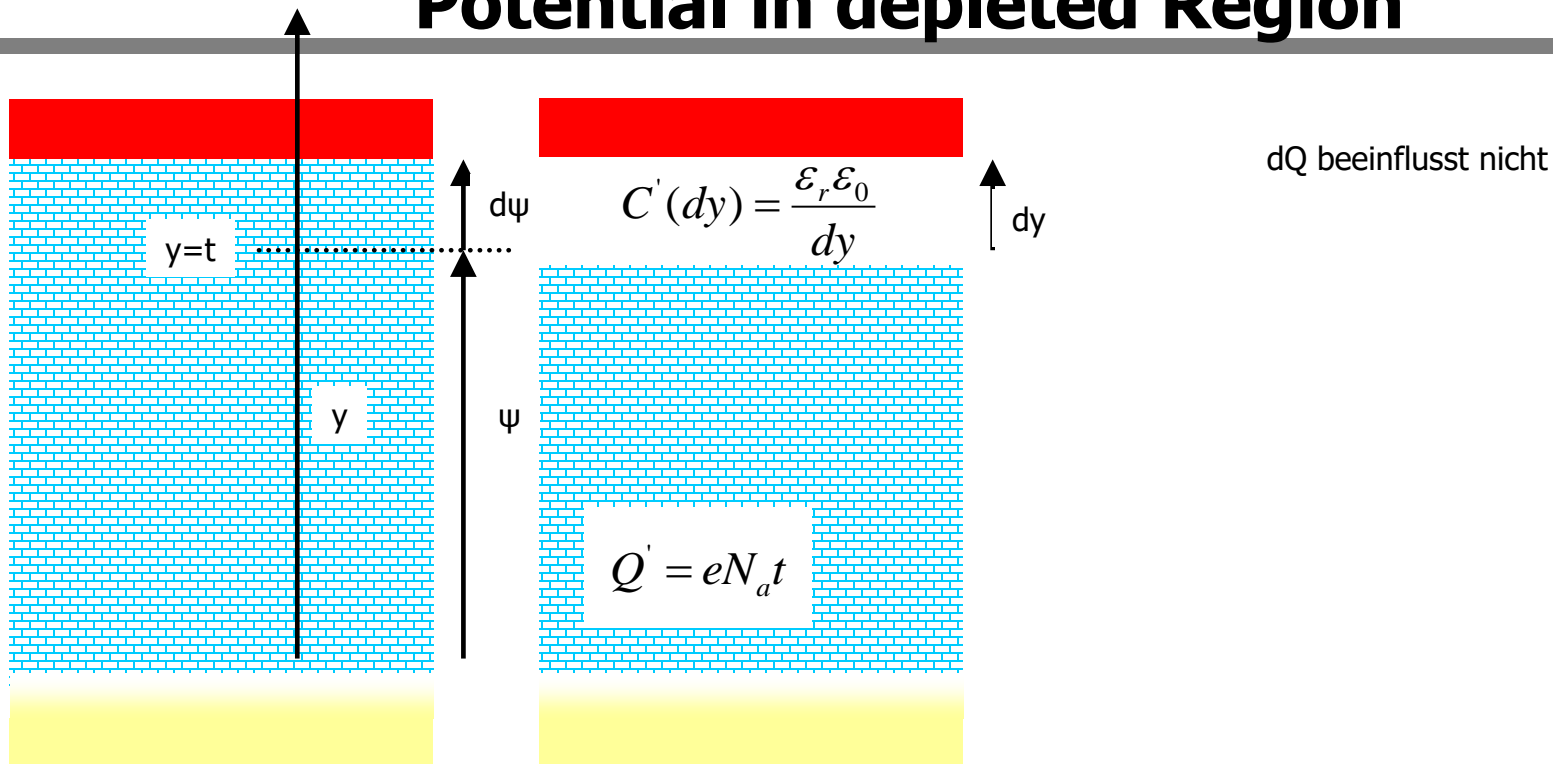
$$\frac{dQ'}{d\psi} = \frac{\epsilon_r \epsilon_0 e N_a}{Q'} \quad Q' dQ' = \epsilon_r \epsilon_0 e N_a d\psi \quad \int \frac{1}{2} Q'^2 = \epsilon_r \epsilon_0 e N_a \psi$$

$$Q' = \sqrt{2\epsilon_r \epsilon_0 e N_a \psi}$$

$$t = \sqrt{\frac{2\epsilon_r \epsilon_0 \psi}{e N_a}}$$

$$C' = \sqrt{\frac{\epsilon_r \epsilon_0 e N_a}{2\psi}}$$

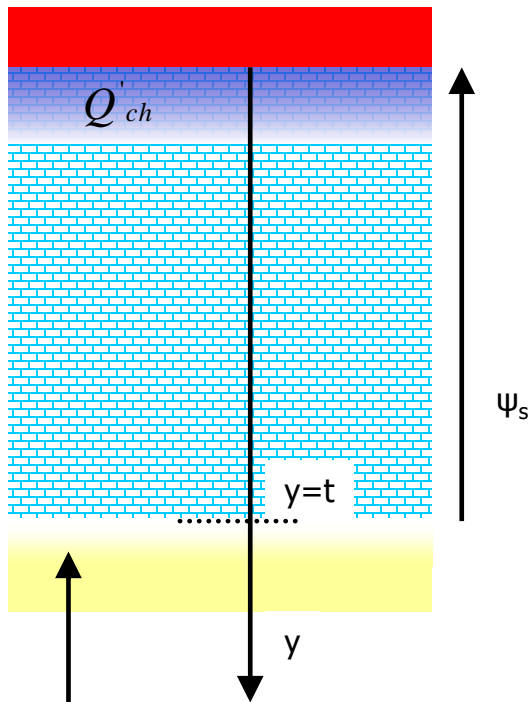
Potential in depleted Region



$$d\psi = \frac{Q'}{C'(dy)} = \frac{eN_a t}{\frac{\epsilon_r \epsilon_0}{dy}} = \frac{eN_a dy}{\frac{\epsilon_r \epsilon_0}{t}} = \frac{eN_a dy}{C'}$$

$$C' = \sqrt{\frac{\epsilon_r \epsilon_0 e N_a}{2\psi}}$$

Charge in Channel



$$p_p = N_a$$

$$n_p = n_i^2 / N_a \equiv n_{p0}$$

$$n_p = en_{p0} e^{\frac{\psi(y)}{U_T}} \quad \psi(y) = \psi_s + \frac{d\psi}{dy} y$$

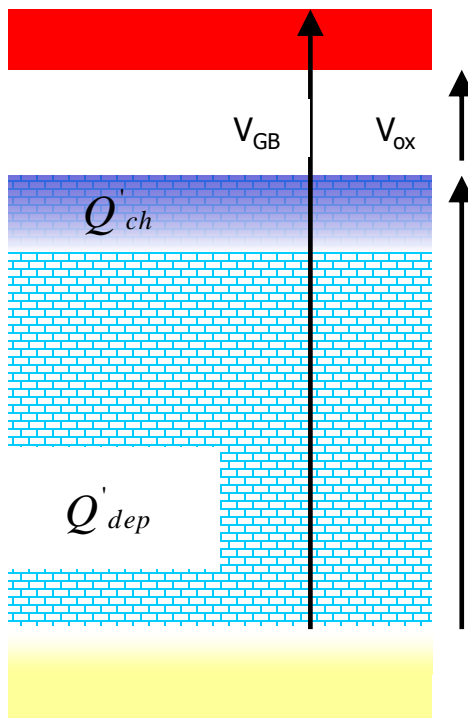
$$n_p = en_{p0} e^{\frac{\psi_s}{U_T}} e^{-\frac{eN_a y}{C'U_T}} \quad Q'_{ch} = \int_0^t en_{p0} e^{\frac{\psi_s}{U_T}} e^{-\frac{eN_a y}{C'U_T}} dy$$

$$Q'_{ch} = \frac{C'U_T}{eN_a} en_{p0} e^{\frac{\psi_s}{U_T}}$$

$$C' = \sqrt{\frac{\epsilon_r \epsilon_0 e N_a}{2\psi_s}}$$

$$\frac{d\psi}{dy} = -\frac{eN_a}{C'}$$

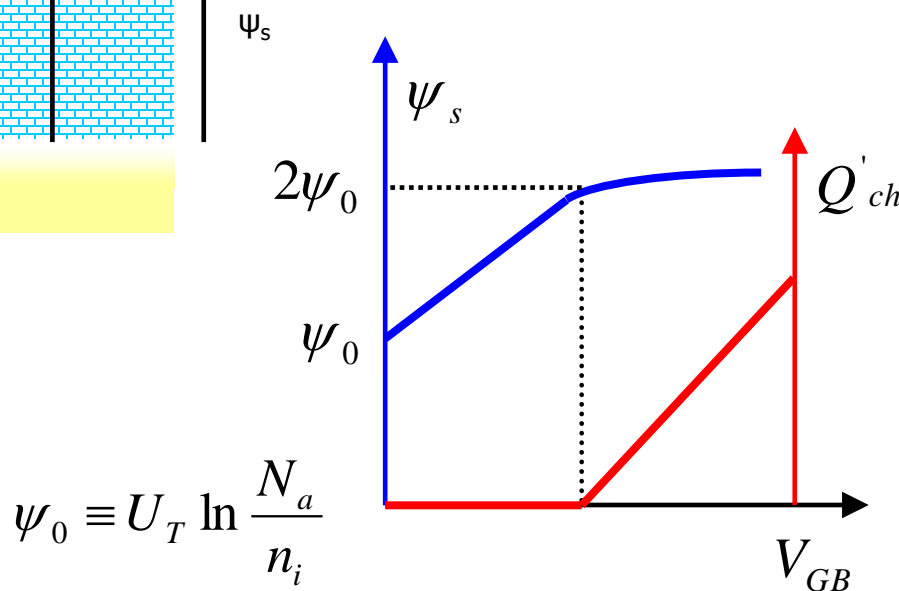
Charge in Channel



$$Q'_{ch} = C'(\psi_s) U_T \frac{n_i^2}{N_a^2} e^{\frac{\psi_s}{U_T}}$$

$$Q'_{dep} = \sqrt{2\epsilon_r \epsilon_0 e N_a \psi_s}$$

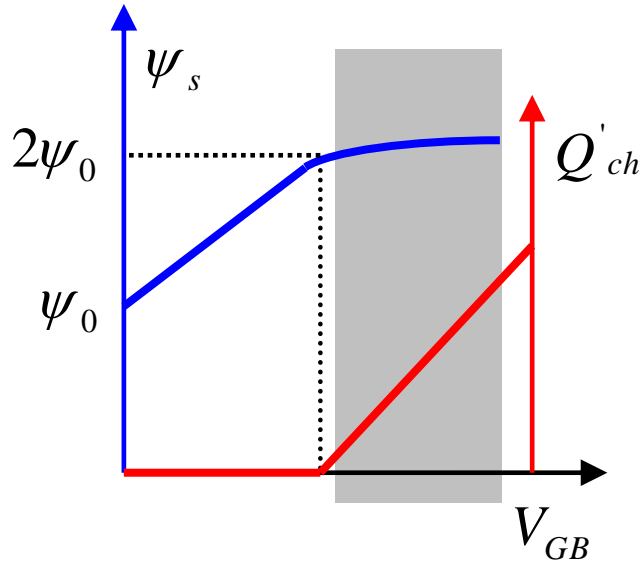
$$V_{GB} = \psi_s + V_{ox} = \psi_s + \frac{Q'_{ch}(\psi_s) + Q'_{dep}(\psi_s)}{C'_{ox}} \quad (+V_{fb}) \quad (-1)$$



$$\psi_0 \equiv U_T \ln \frac{N_a}{n_i}$$

$$\psi_0 \equiv U_T \ln \frac{N_a}{n_i} = 0.42V$$

strong Inversion



$$\psi_0 \equiv U_T \ln \frac{N_a}{n_i}$$

$$Q'_{ch} = C'(\psi_s) U_T \frac{n_i^2}{N_a^2} e^{\frac{\psi_s}{U_T}}$$

$$Q'_{dep} = \sqrt{2\epsilon_r \epsilon_0 e N_a \psi_s}$$

$$\psi_s \approx 2\psi_0 = 2U_T \ln \frac{N_a}{n_i}$$

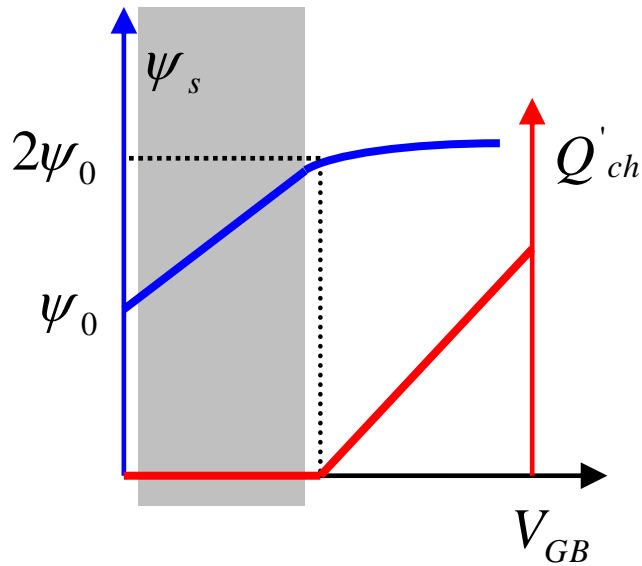
$$V_{GB} = \psi_s + \frac{Q'_{ch}(\psi_s) + Q'_{dep}(\psi_s)}{C'_{ox}}$$

$$V_{GB} = 2\psi_0 + \frac{Q'_{ch} + Q'_{dep}(2\psi_0)}{C'_{ox}} \leftarrow 2\psi_0 + 6U_T$$

$$V_{TH} = V_{GB}(2\psi_0) = 2\psi_0 + \frac{Q'_{dep}(2\psi_0)}{C'_{ox}}$$

$$Q'_{ch} = C'_{ox}(V_{GB} - V_{TH})$$

Weak Inversion



$$\psi_0 \equiv U_T \ln \frac{N_a}{n_i}$$

$$Q'_{ch} = C'(\psi_s) U_T \frac{n_i^2}{N_a^2} e^{\frac{\psi_s}{U_T}}$$

$$Q'_{dep} = \sqrt{2\epsilon_r \epsilon_0 e N_a \psi_s}$$

$$Q'_{ch} \ll Q'_{dep}$$

$$V_{GB} = \psi_s + \frac{Q'_{ch}(\psi_s) + Q'_{dep}(\psi_s)}{C'_{ox}}$$

$$V_{GB}(\psi_s) = \psi_s + \frac{Q'_{dep}(\psi_s)}{C'_{ox}}$$

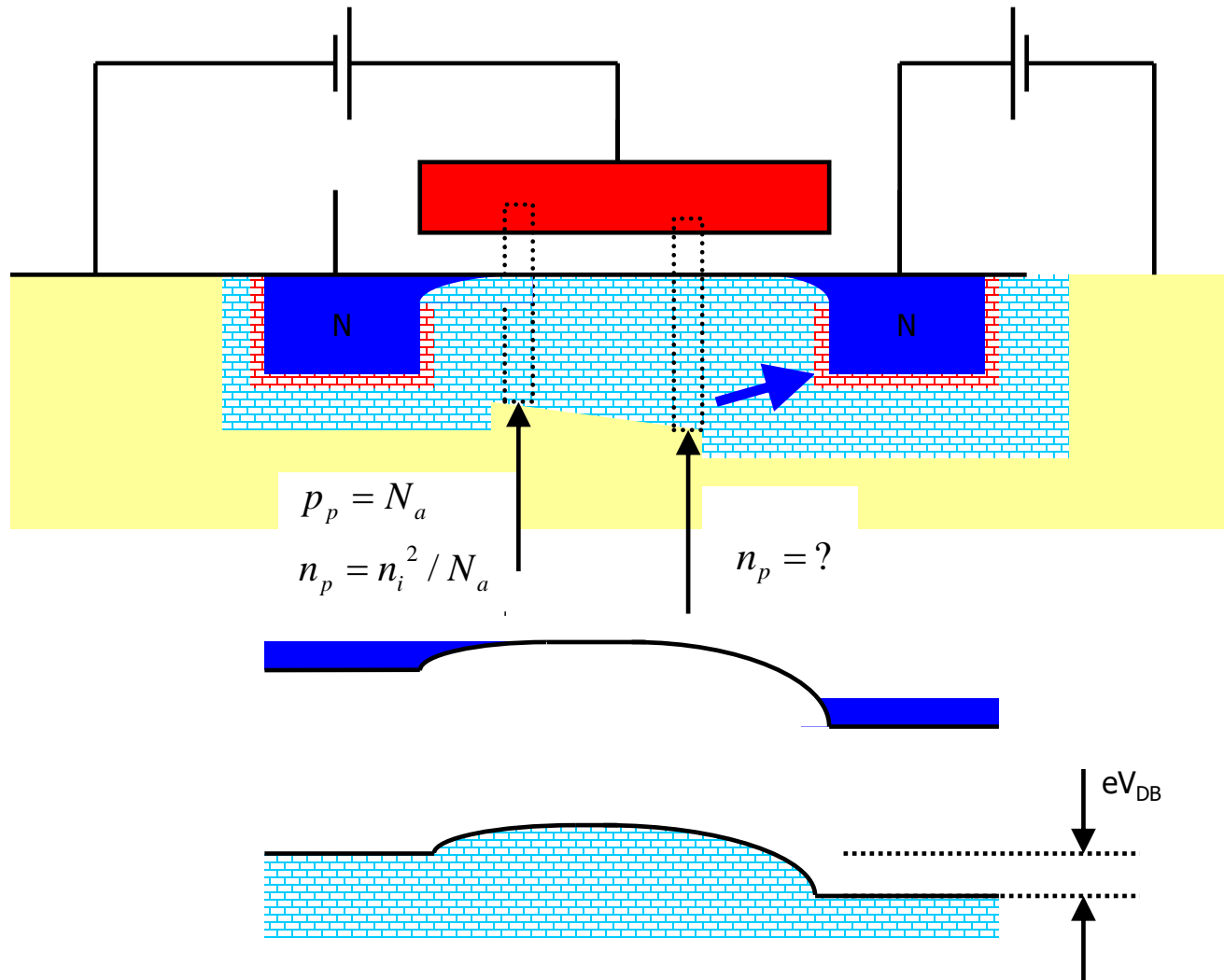
$$C' = \frac{dQ_{dep}}{d\psi_s}$$

$$V_{GB} = V_{GB}(2\psi_0) + \left. \frac{dV_{GB}}{d\psi_s} \right|_{2\psi_0} (2\psi_0 - \psi_s)$$

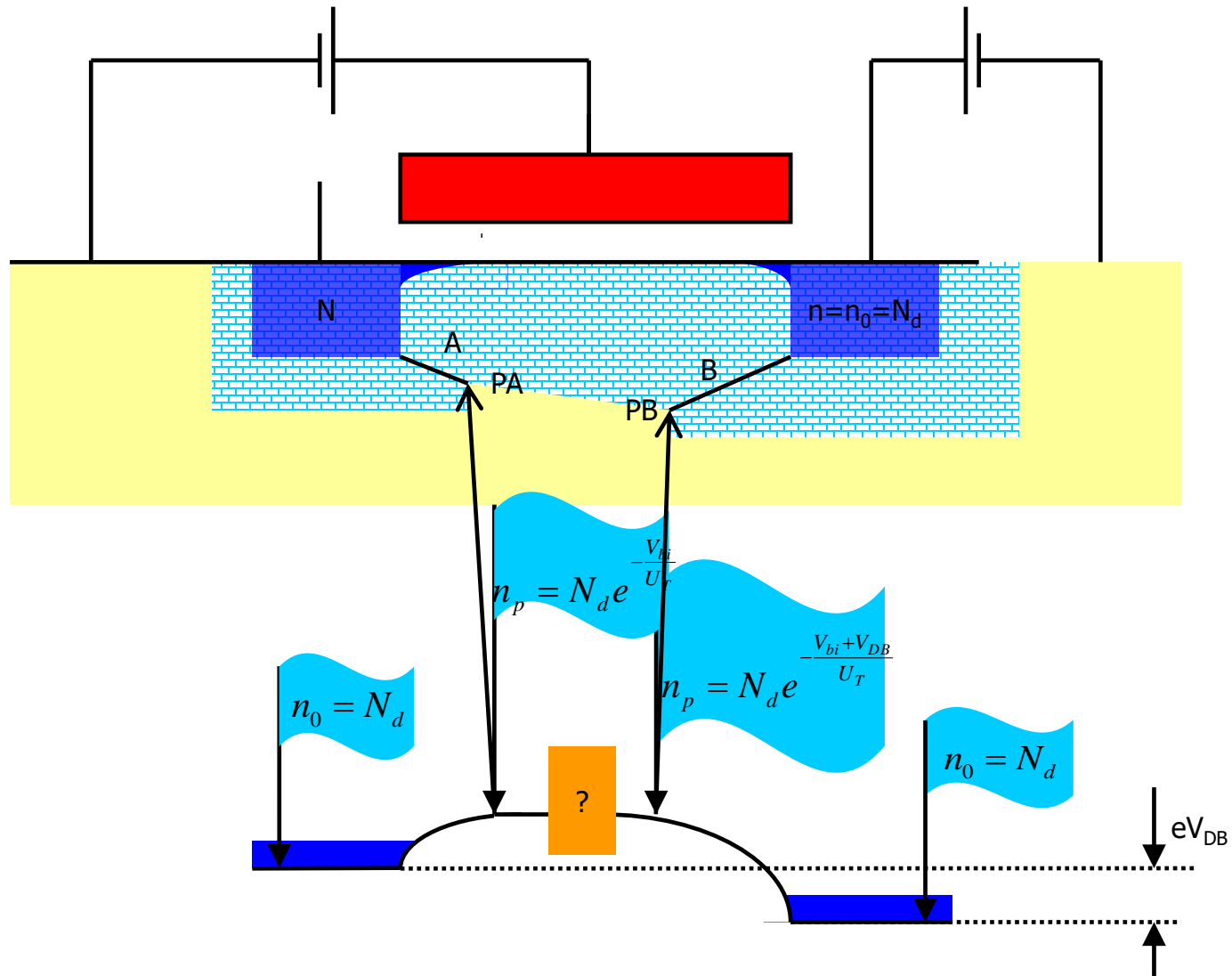
$$\psi_s = 2\psi_0 + \frac{V_{GB} - V_{TH}}{n} \quad 1 + \frac{C'(2\psi_0)}{C'_{ox}} \equiv n$$

$$Q'_{ch} \approx (n-1) C'_{ox} U_T e^{\frac{V_{GB} - V_{TH}}{n U_T}}$$

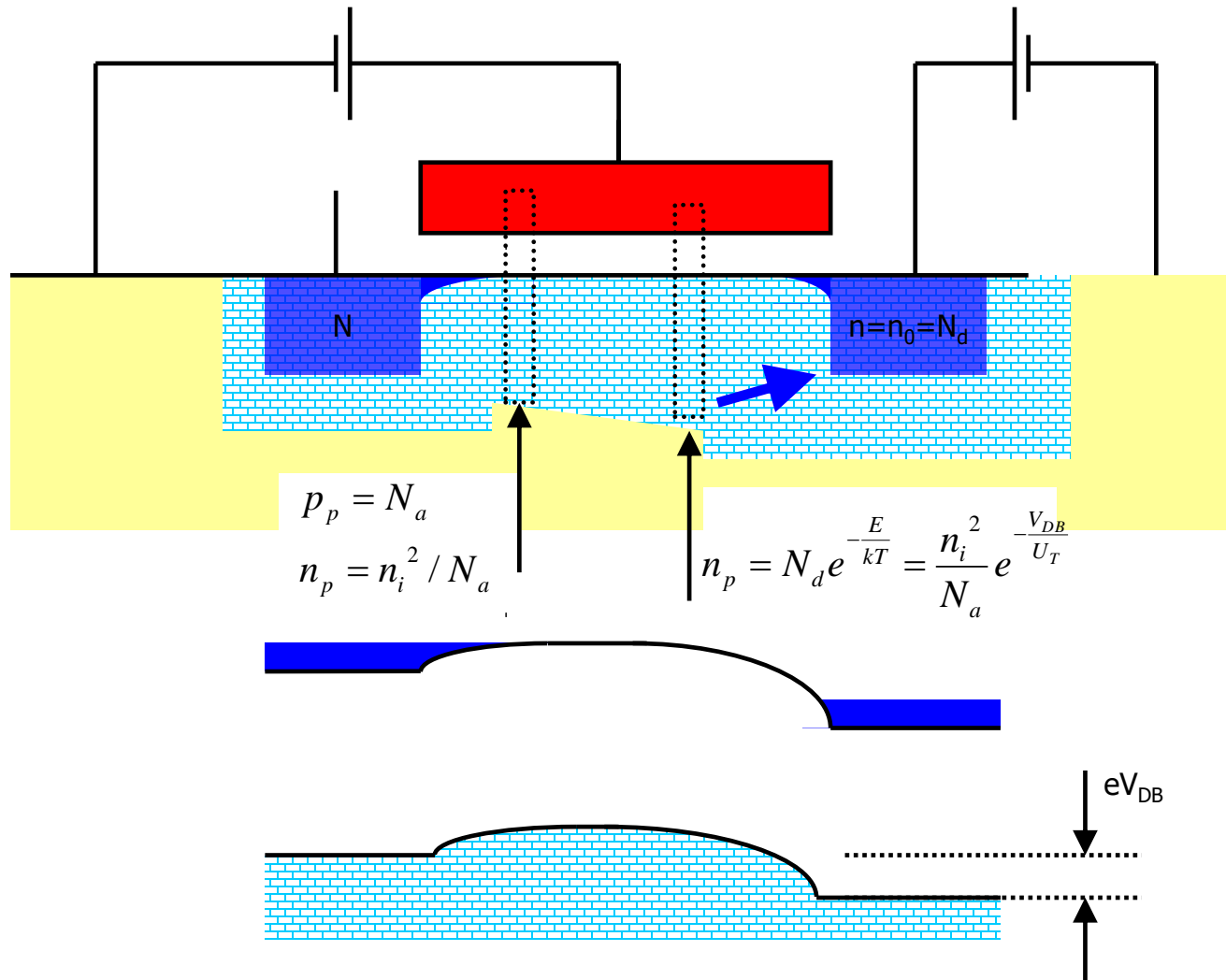
Drain Bias



Drain Bias



Drain Bias



Drain Bias

$$\psi_0 \equiv U_T \ln \frac{N_a}{n_i}$$

$$V_{TH} = V_{GB}(2\psi_0) = 2\psi_0 + \frac{Q'_{dep}(2\psi_0)}{C'_{ox}}$$

$$Q'_{ch} = C'_{ox}(V_{GB} - V_{TH})$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GB}-V_{TH}}{nU_T}}$$

$$\frac{n_i^2}{N_a} \rightarrow \frac{n_i^2}{N_a} e^{-\frac{V_{DG}}{U_T}}$$

$$2\psi_0 \rightarrow 2\psi_0 + V_{DB}$$

$$V_{TH} \rightarrow V_{TH} + nV_{DB}$$

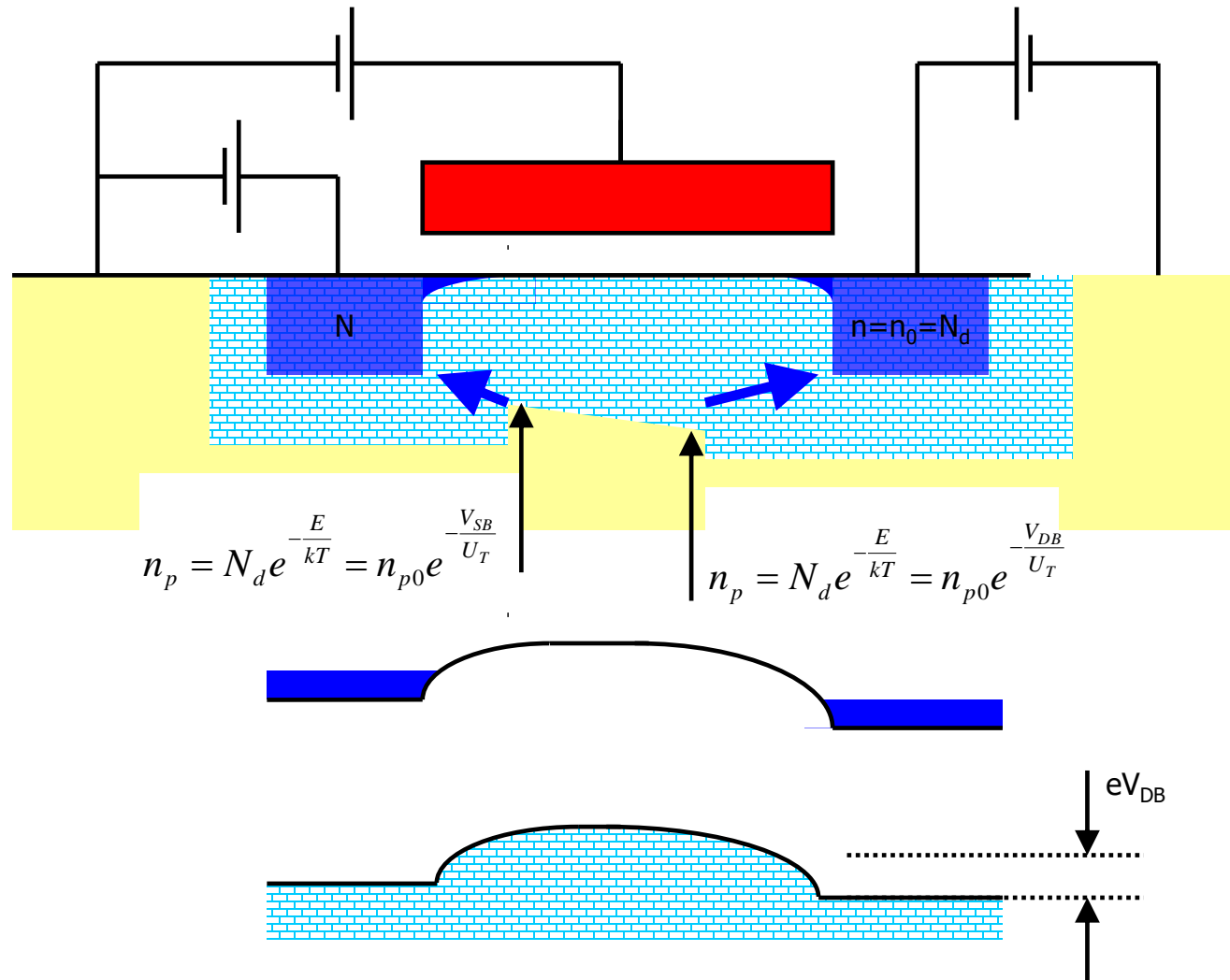
$$Q'_{ch} \approx C'_{ox}(V_{GB} - V_{TH} - nV_{DB})$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GB}-V_{TH}}{nU_T}} e^{-\frac{V_{DB}}{U_T}}$$

$$V_{TH} = V_{GB}(2\psi_0) = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a2\psi_0}}{C'_{ox}}$$

$$1 + \frac{C'(2\psi_0)}{C'_{ox}} \equiv n$$

Drain and Source Bias



Charge in Channel

$$Q'_{ch} \approx C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$V_x \in (0, V_{DS})$$

$$V_{TH} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0 eN_a(2\psi_0 + V_{SB})}}{C'_{ox}}$$

$$1 + \frac{C'(2\psi_0 + V_{SB})}{C'_{ox}} \equiv n$$

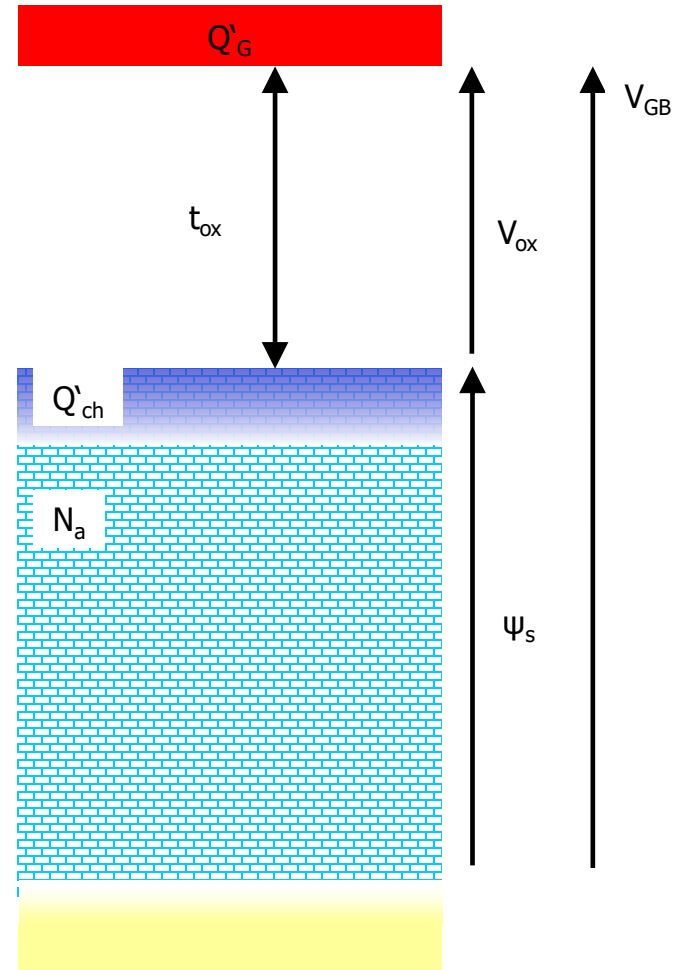
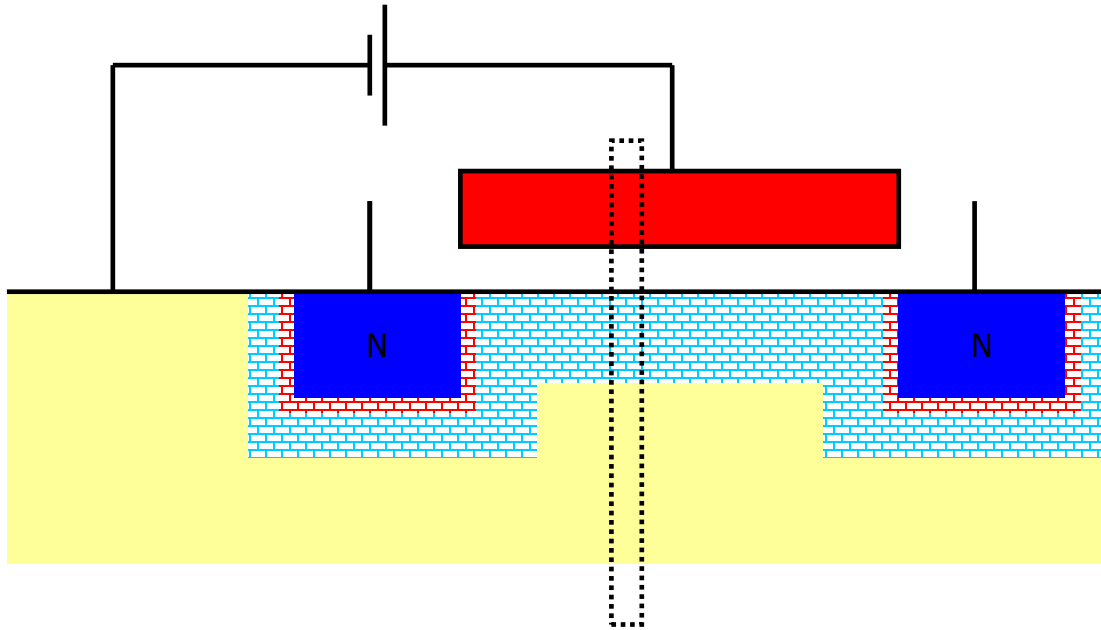
$$Q'_{ch} \approx C'_{ox}(V_{GB} - V_{TH0} - nV_x)$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GB}-V_{TH0}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$V_x \in (V_{SB}, V_{DB})$$

$$V_{TH0} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0 eN_a(2\psi_0)}}{C'_{ox}}$$

Gate Bias



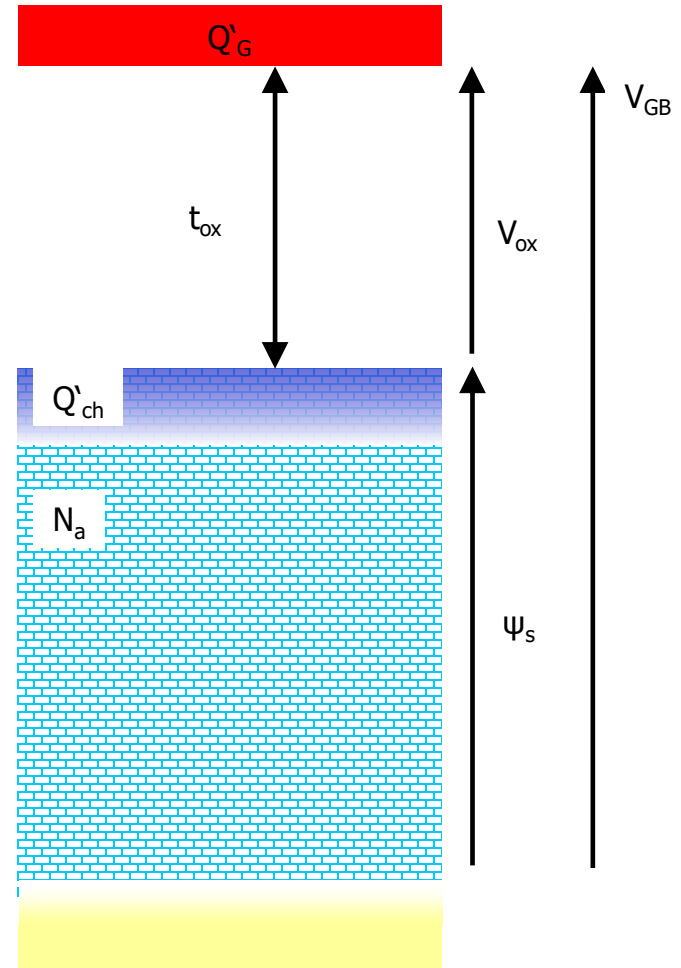
Gate Bias

$$V_{TH} = V_{GB}(2\psi_0) = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a2\psi_0}}{C'_{ox}}$$

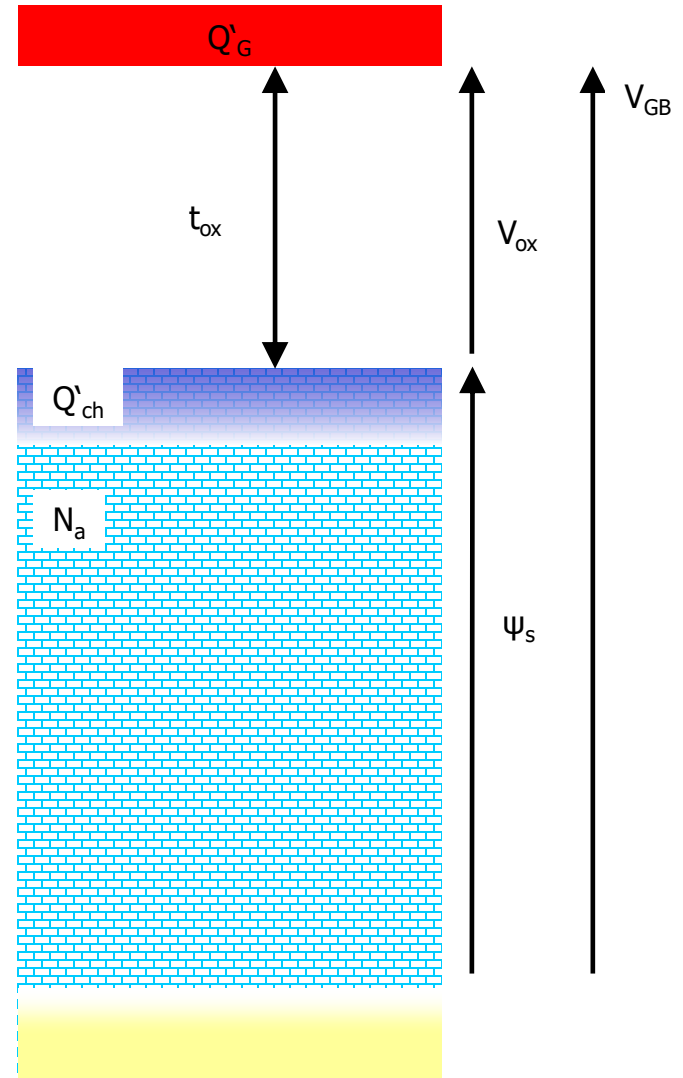
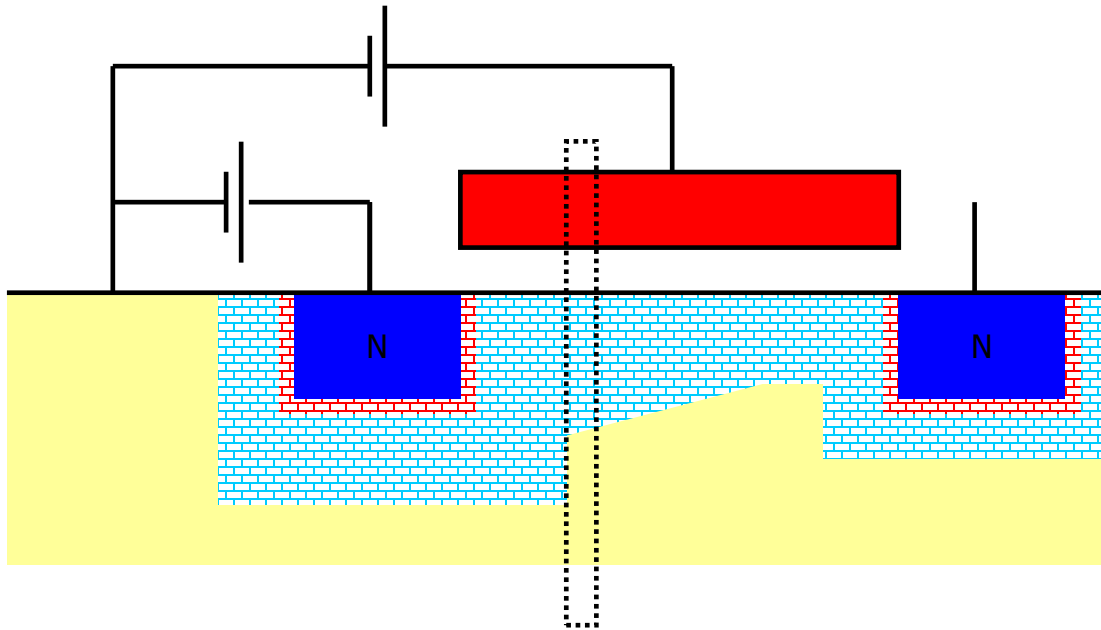
$$Q'_{ch} = C'_{ox}(V_{GB} - V_{TH})$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GB}-V_{TH}}{nU_T}}$$

$$1 + \frac{C'(2\psi_0)}{C'_{ox}} \equiv n$$



Source Bias



$$\psi_s = 2\psi_0$$

$$\psi_s = 2\psi_0 + V_{SB}$$

Source Bias

$$V_{TH} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a(2\psi_0 + V_{SB})}}{C'_{ox}}$$

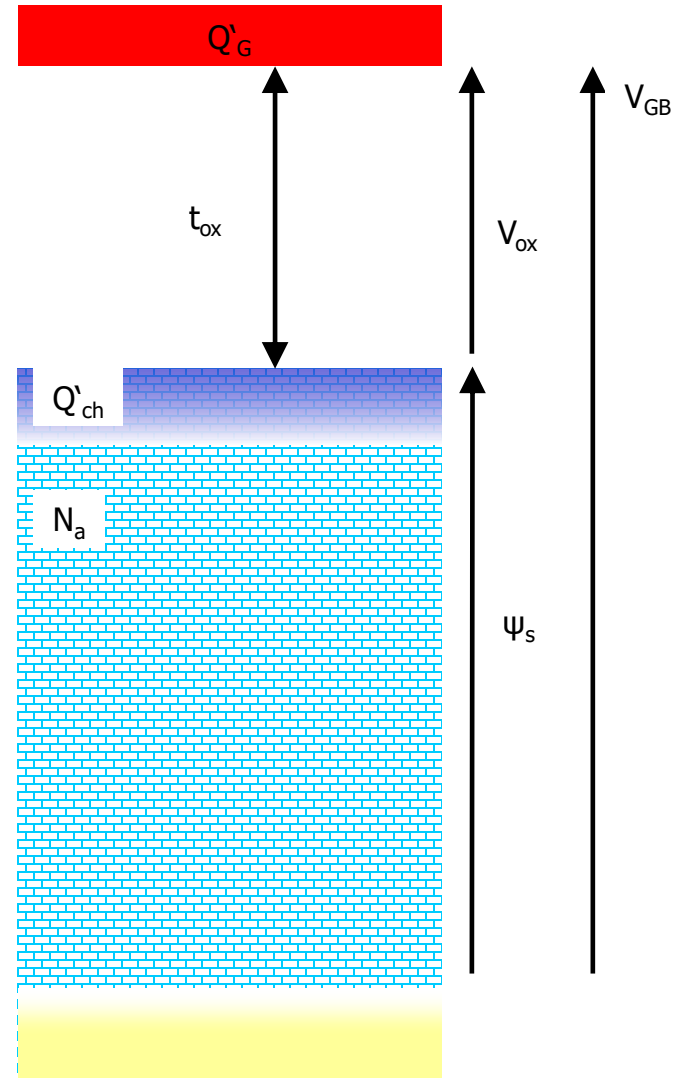
$$Q'_{ch} = C'_{ox}(V_{GS} - V_{TH})$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}}$$

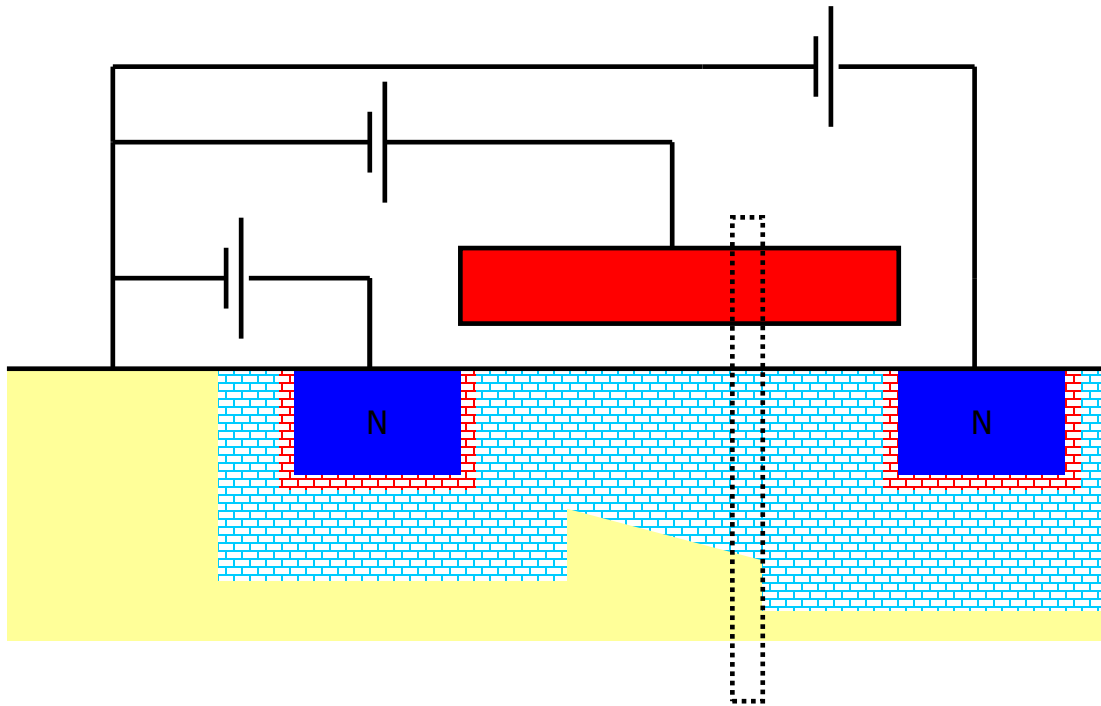
$$1 + \frac{C'(2\psi_0 + V_{SB})}{C'_{ox}} \equiv n$$

$$V_{TH0} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a 2\psi_0}}{C'_{ox}}$$

$$Q'_{ch} = C'_{ox}(V_{GB} - V_{TH0} - nV_{SB})$$



Drain Bias



Drain Bias

$$V_{TH} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a(2\psi_0 + V_{SB})}}{C'_{ox}}$$

$$Q'_{ch} = C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$1 + \frac{C'(2\psi_0 + V_{SB})}{C'_{ox}} \equiv n$$

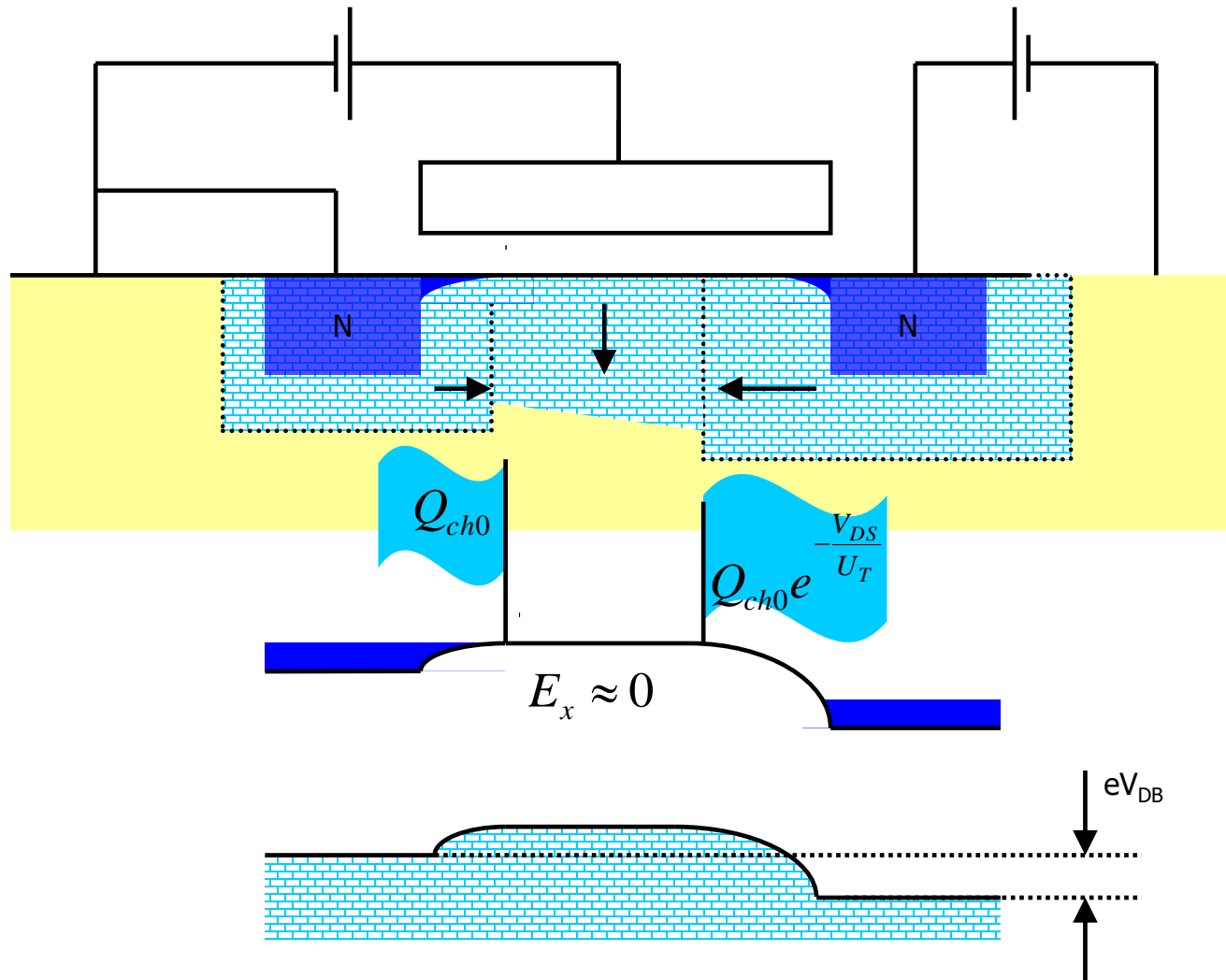
$$V_{TH0} = 2\psi_0 + \frac{\sqrt{2\varepsilon_r\varepsilon_0eN_a2\psi_0}}{C'_{ox}}$$

$$Q'_{ch} = C'_{ox}(V_{GB} - V_{TH0} - nV_x)$$

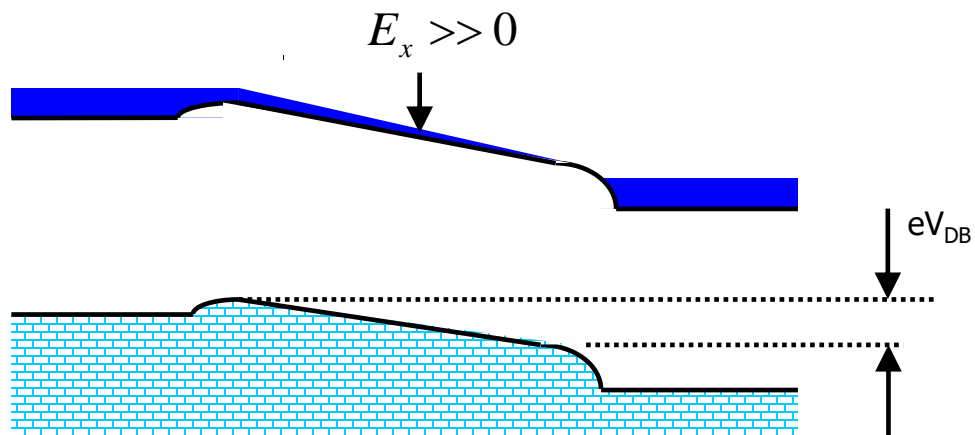
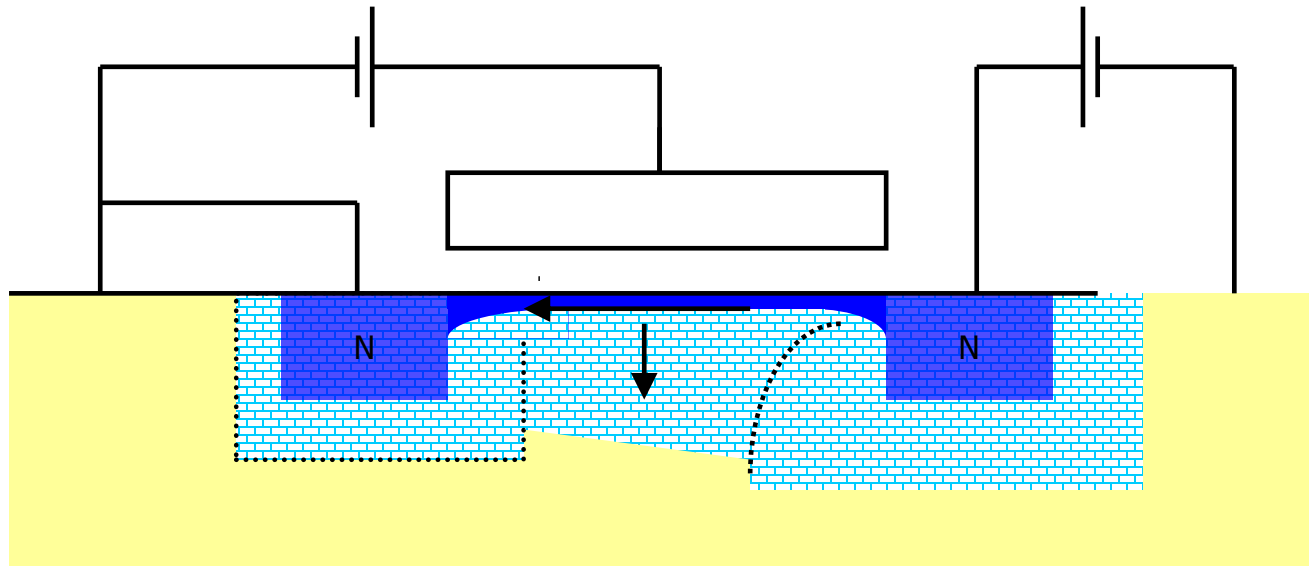
$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GB}-V_{TH0}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$V_x \in (V_{SB}, V_{DB})$$

Weak Inversion



Strong Inversion



Strong Inversion - Drain Current

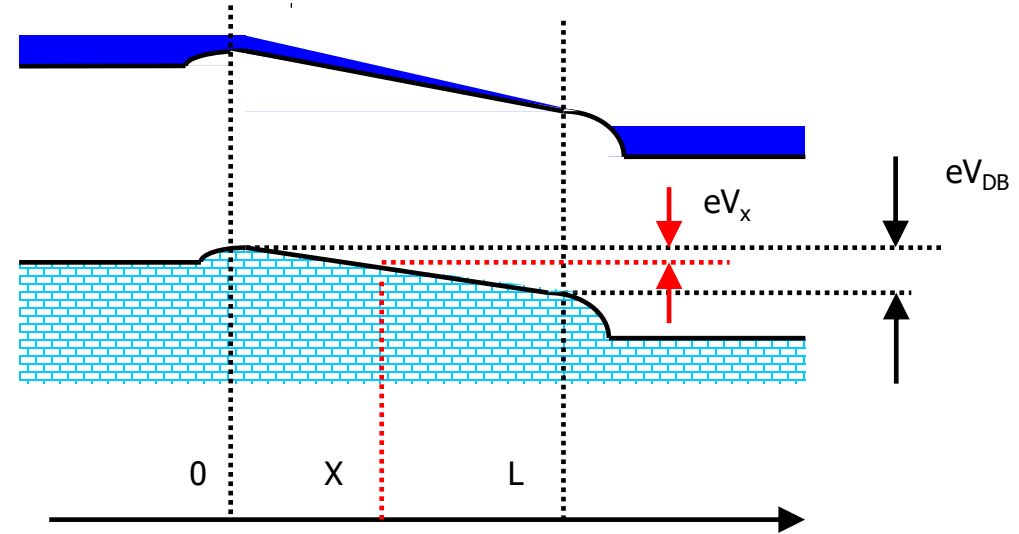
$$I(x) = W\mu Q'_{ch} \frac{dV_x}{dx} = \text{const}(x)$$

$$\int Idx = \int W\mu Q'_{ch} \frac{dV_x}{dx} dx$$

$$\int_0^L Idx = \int_0^{V_{DS}} W\mu Q'_{ch} dV_x$$

$$IL = \int_0^{V_{DS}} W\mu Q'_{ch} dV_x$$

$$I = \mu \frac{W}{L} \int_0^{V_{DS}} Q'_{ch} dV_x$$



$$Q'_{ch} \approx C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

Weak Inversion - Drain Current

$$I(x) = -WD \frac{dQ'_{ch}}{dx} = \text{const}(x)$$

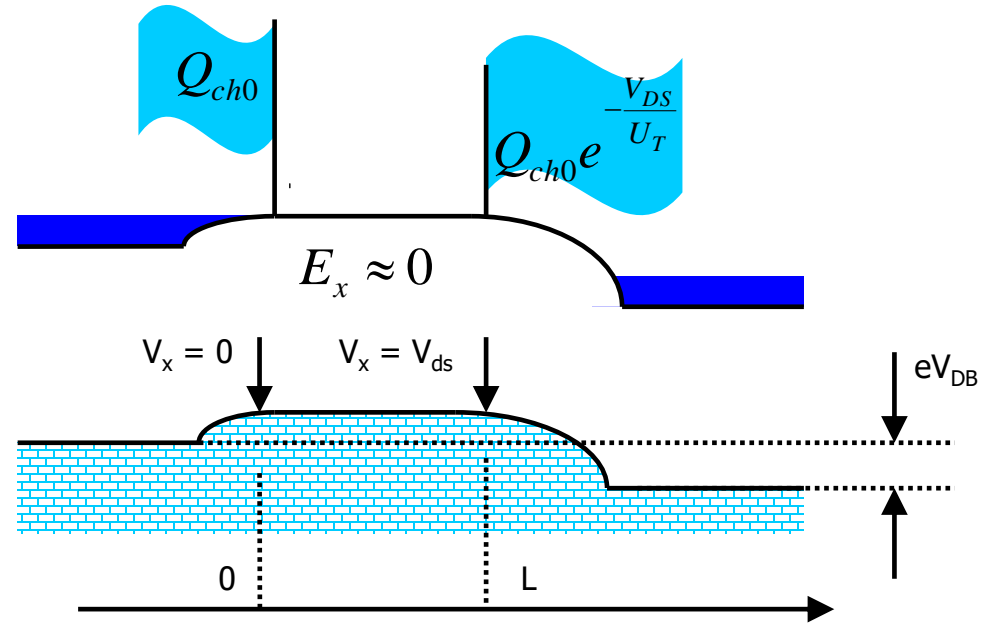
$$\int I(x) dx = -\int WD \frac{dQ'_{ch}}{dx} dx$$

$$\int_0^L Idx = -\int_0^{V_{DS}} WD \frac{dQ'_{ch}}{dV_x} dV_x$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$LI = \int_0^{V_{DS}} W \frac{D}{U_T} Q'_{ch} dV_x$$

$$I = \mu \frac{W}{L} \int_0^{V_{DS}} Q'_{ch} dV_x$$



Strong- and Weak Inversion

$$I = \mu \frac{W}{L} \int_0^{V_{DS}} Q'_{ch} dV_x$$

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

$$I = \mu C'_{ox} \frac{W}{L} (n-1)U_T^2 e^{\frac{V_{GST}}{nU_T}} \left(1 - e^{-\frac{V_{DS}}{U_T}} \right)$$

$$Q'_{ch} \approx C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

$$I = \mu C'_{ox} \frac{W}{L} \left(V_{GST}V_{DS} - n \frac{V_{DS}^2}{2} \right)$$

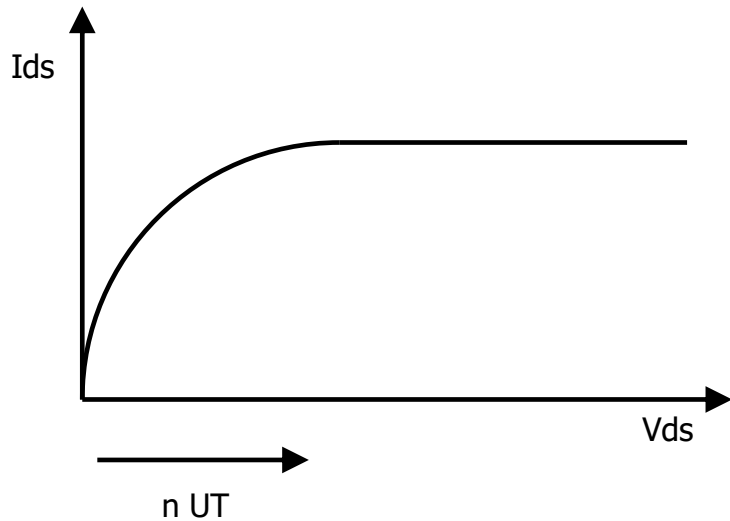
$$I = \mu C'_{ox} \frac{W}{L} \left[(V_{GBT} - nV_{SB})^2 - (V_{GBT} - nV_{DB})^2 \right]$$

$$V_{GST} \equiv V_{GS} - V_T; V_{GBT} \equiv V_{GB} - V_{T0}$$

Weak Inversion

$$Q'_{ch} \approx (n-1)C'_{ox}U_T e^{\frac{V_{GS}-V_{TH}}{nU_T}} e^{-\frac{V_x}{U_T}}$$

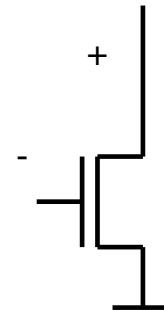
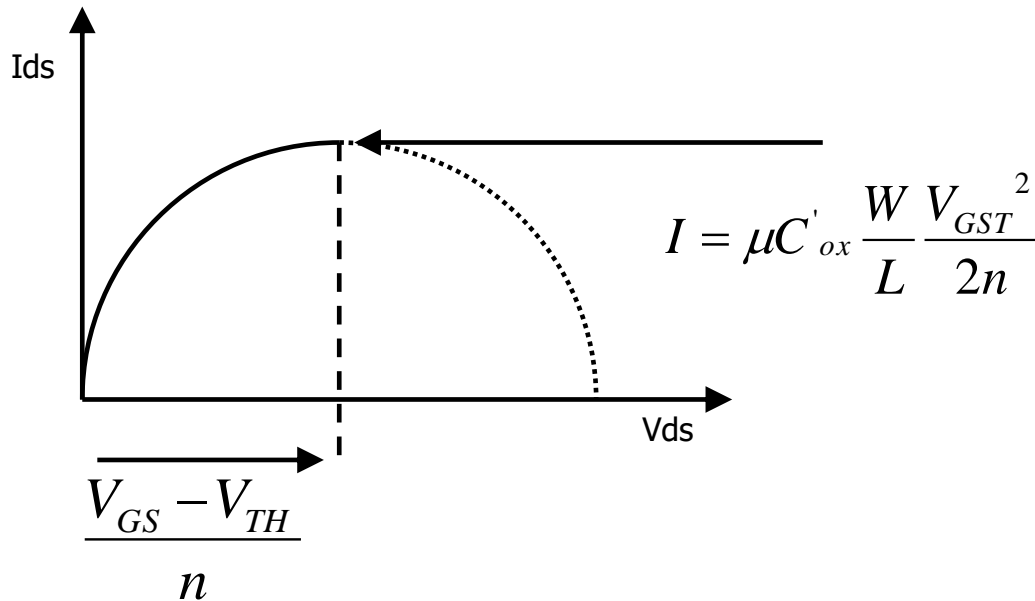
$$I = \mu C'_{ox} \frac{W}{L} (n-1)U_T^2 e^{\frac{V_{GS}}{nU_T}} \left(1 - e^{-\frac{V_{DS}}{U_T}} \right)$$



Strong Inversion

$$Q'_{ch} \approx C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

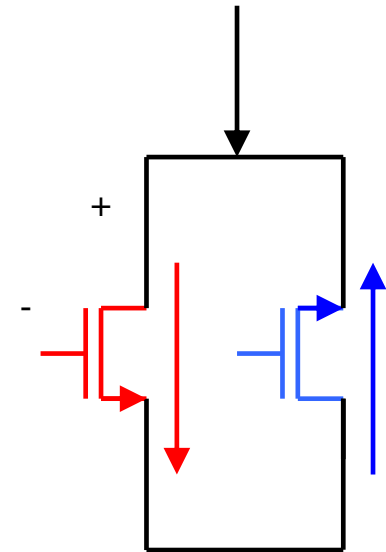
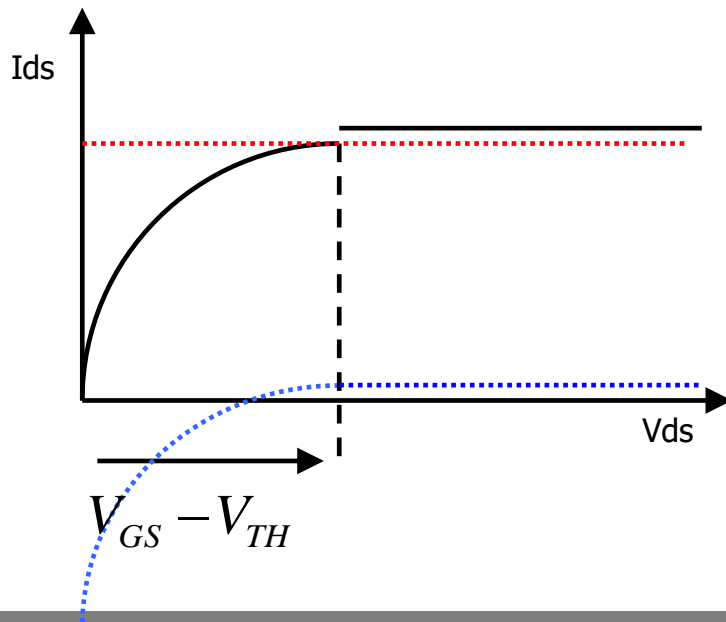
$$I = \mu C'_{ox} \frac{W}{L} \left(V_{GST} V_{DS} - n \frac{V_{DS}^2}{2} \right)$$



EKV

$$I = \mu C'_{ox} \frac{W}{L} \left[(V_{GBT} - nV_{SB})^2 - (V_{GBT} - nV_{DB})^2 \right]$$

$$V_{GST} \equiv V_{GS} - V_T; V_{GBT} \equiv V_{GB} - V_{T0}$$



BSIM - Drain Current

$$I(x) = W\mu Q'_{ch} \frac{dV_x}{dx} = \text{const}(x) \quad Q'_{ch} \approx C'_{ox}(V_{GS} - V_{TH} - nV_x)$$

$$v = \mu E_x \quad E_x < E_{sat} \quad \mu = \frac{\mu_0}{1 + E_x / E_{sat}}$$

$$E_x > E_{sat} \quad v = v_{sat} = \frac{\mu_0}{2} E_{sat}$$

$$\int I \left(1 + \frac{1}{E_{sat}} \frac{dV_x}{dx} \right) dx = \int W\mu_0 Q'_{ch} \frac{dV_x}{dx} dx$$

$$I = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{DS}}{LE_{sat}} \right)} \left(V_{GST} - n \frac{V_{DS}^2}{2} \right)$$

BSIM - Saturation

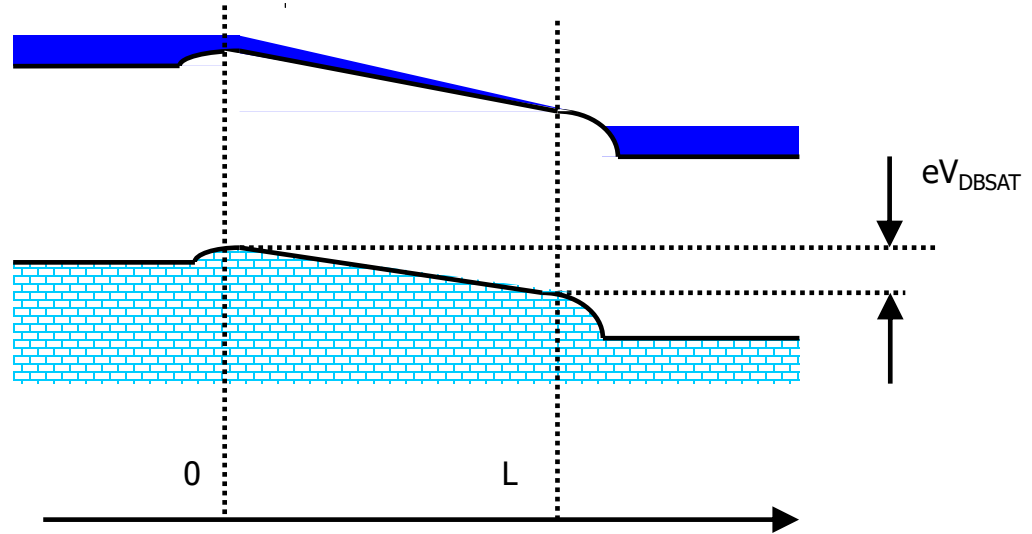
$$I = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{DS}}{LE_{sat}} \right)} \left(V_{GST} - n \frac{V_{DS}^2}{2} \right)$$

$$I_{sat} = v_{sat} W Q'_{ch}(L)$$

$$Q'_{ch} \approx C'_{ox} (V_{GST} - nV_x)$$

$$I_{sat} = \frac{\mu_0}{2} E_{sat} W C'_{ox} (V_{GST} - nV_{DSSAT})$$

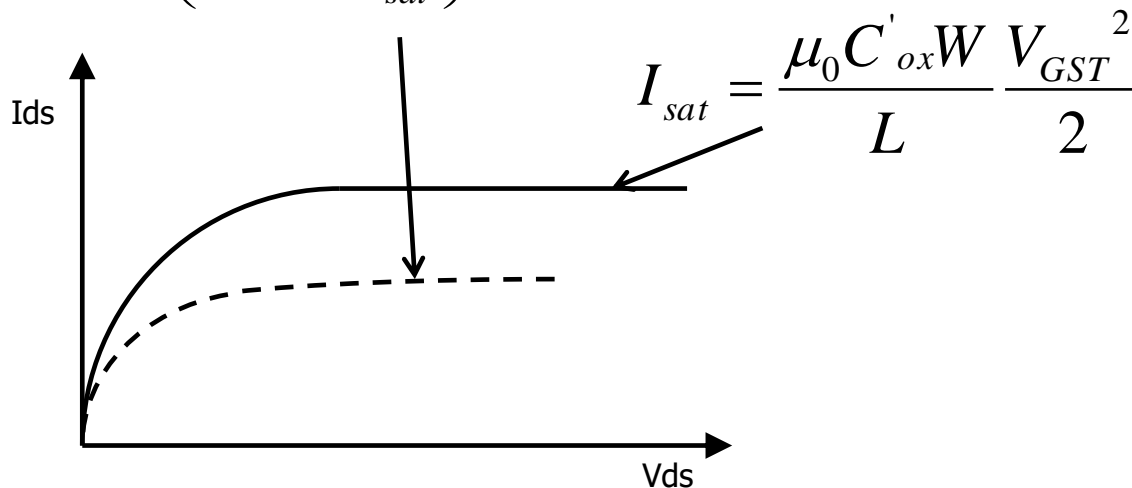
$$\frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{DSSAT}}{LE_{sat}} \right)} \left(V_{GST} - n \frac{V_{DSSAT}^2}{2} \right) = \frac{\mu_0}{2} E_{sat} C'_{ox} W (V_{GST} - nV_{DSSAT})$$



BSIM - Saturation

$$V_{DSSAT} = \frac{V_{GST}}{n \left(1 + \frac{V_{GST}}{nLE_{sat}} \right)}$$

$$I_{sat} = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{GST}}{nLE_{sat}} \right)} \frac{V_{GST}^2}{2n}$$



$$U_T = 26mV$$

$$\epsilon_{si} = 11\epsilon_0$$

$$2\psi_0 = 0.85V$$

$$C'_{ox} = 3fF / \mu m^2$$

$$\mu_{n0} = 0.067m^2 / Vs$$

$$\mu_{p0} = 0.025m^2 / Vs$$

$$E_{sn} = 2.4V / \mu m$$

$$E_{sp} = 6.4V / \mu m$$

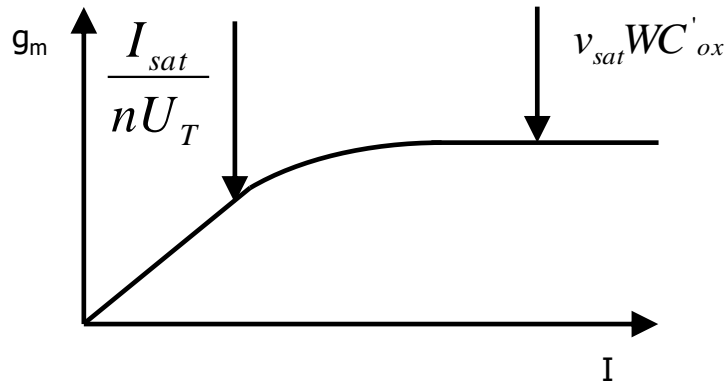
$$V_{TH} = 0.57V$$

$$n = 1.42$$

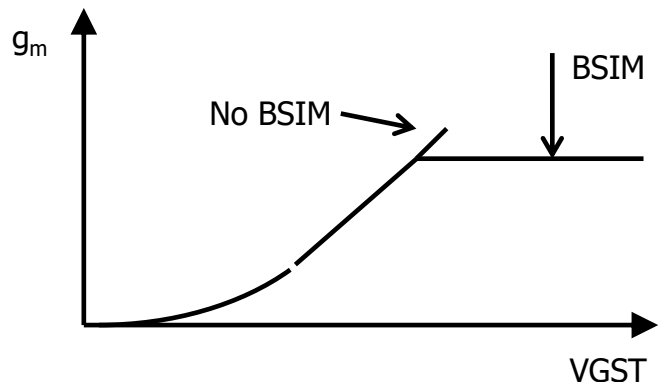
Trans-conductance

$$I_{sat} = \mu C'_{ox} \frac{W}{L} (n-1) U_T^2 e^{\frac{V_{GST}}{nU_T}}$$

$$I_{sat} = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{GST}}{nLE_{sat}} \right)} \frac{V_{GST}^2}{2n}$$



$$I_{sat} = \frac{\mu_0 C'_{ox} W}{L} \frac{V_{GST}^2}{2n}$$



$$I_{sat} = \frac{\mu_0}{2} E_{sat} WC'_{ox} V_{GST} = v_{sat} WC'_{ox} V_{GST}$$

BSIM – Early Effekt

$$I = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{DS}}{LE_{sat}} \right)} \left(V_{GST} - n \frac{V_{DS}^2}{2} \right)$$

$$I_{sat} = \frac{\mu_0 C'_{ox} W}{L \left(1 + \frac{V_{GST}}{nLE_{sat}} \right)} \frac{V_{GST}^2}{2n}$$

$$I = I_{sat} + \left. \frac{\partial I}{\partial V_{DS}} \right|_{V_{DSSAT}} (V_{DS} - V_{DSSAT})$$

$$I = I_{sat} \left(1 + \frac{V_{DS} - V_{DSSAT}}{V_A} \right)$$

$$V_A = LE_{sat} + V_{DSSAT}$$

